#### AN IMPLEMENTATION OF PEAK TO AVERAGE POWER RATIO REDUCTION FOR MULTICARRIER SYSTEM (ORTHOGONAL FREQUENCY DIVISION MULTIPLEXING)

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A thesis submitted in fulfillment of the requirement for the award of the Degree Masters in Electrical and Electronic Engineering

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> > June 2015

**DEDICATION** 

# er dears er ... A Market Anders PERPUSTAKAAN Dedicate this work to my mother and my father dears

#### ACKNOWLEDGEMENT

All praise for Allah S.W.T, blessings to Prophet Muhammad S.A.W along with his family and friends. Thanks to Allah because gave this permission to me prepared and accomplished this master thesis in the title "An Implementation of Peak to Average Power Ratio Reduction for Multicarrier System (Orthogonal Frequency Division Multiplexing)" in its time.

In this opportunity I am heartily thankful to my supervisor, **Dr. Khairun Nidzam Bin Ramli**, whose encouragement, supervision and support from the preliminary to the concluding level enabled me to develop an understanding until accomplished this thesis.



Special thanks for my great family who were by dint of blessings their calls and support until successes.

#### ABSTRACT

Orthogonal frequency division multiplexing (OFDM) has been becoming more popular modulation technique in the high-speed wireless communication system. It is used especially in Large Term Evaluation technique (LTE) which depended from the fourth-generation (4G) of wireless communication system. OFDM proves high efficiency to transmit data rate as high as 100 Mbps, the capability to combat multipath fading channel and utilization the whole bandwidth. Although, OFDM technology has more advantages, the same time has some obstacles also.

The highest Peak to average power ratio (PAPR) considers the main restrict which cause non-linearity at receiving end. Coding, clipping and phase rotation among many PAPR reduction techniques are proposed to overcome this problem. In this project, we investigated the PAPR reduction performance with two PAPR reduction techniques selective mapping (SLM) and partial transmit sequence (PTS). These two PAPR reduction methods consider sub-parts of signal scrambling technique that depend on phase rotation technique in its operation.

The simulation results show SLM and PTS methods have improved the PAPR reduction performance with different parameters. Moreover, different kinds of SLM and PTS schemes are also plotted. Generally, PTS and SLM techniques are leading the PAPR reduction better performance. The results are verified using MATLAB software.



#### ABSTRAK

Frekuensi Ortogon Bahagian Pemultipleksan (OFDM) merupakan teknik modulasi yang semakin popular dalam sistem komunikasi pantas tanpa wayar terutamanya teknik *Large Term Evaluation* (LTE) yang berasaskan kepada sistem komunikasi tanpa wayar 4G. OFDM terbukti mempunyai keberkesanan yang tinggi untuk menghantar data dengan kadar sehingga 100 Mbps, keupayaan untuk melalui saluran pudar pelbagai arah dan penggunaan kesemua lebar jalur. Walaupun teknologi OFDM mempunyai banyak kelebihan, tetapi pada masa yang sama ia juga mempunyai banyak kekangan.

Nisbah Kuasa Puncak ke Kuasa Purata (PAPR) merupakan kekangan utama yang menyebabkan keadaan tak linear pada bahagian penerima. Pengkodan, keratan dan putaran fasa diantara kebanyakan teknik pengurangan PAPR diutarakan untuk mengatasi masalah tersebut. Dalam projek ini, prestasi pengurangan PAPR telah dikaji dengan dua teknik PAPR iaitu *selective mapping* (SLM) dan *Partial Transmit Sequence* (PTS). Kedua- dua teknik pengurangan PAPR ini boleh dikatakan pecahan dari teknik gegasan isyarat yang berdasarkan kepada teknik putaran fasa dalam operasinya.

Keputusan simulasi menunjukkan kaedah SLM dan PTS telah meningkatkan prestasi pengurangan PAPR pada parameter yang berlainan. Tambahan lagi, jenis – jenis skim SLM dan PTS yang berlainan juga dipaparkan pada graf. Umumnya, teknik SLM dan PTS menunjukkan pencapaian yang lebih baik untuk pengurangan PAPR. Keputusan dibuktikan menggunakan perisian MATLAB.



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### LIST OF ABBREVIATION AND SYMBOLS

	2G	Second Generation
	3G	Third Generations
	4G	Fourth Generation
	IP	Internet Protocol
	OFDM	Orthogonal Frequency Division Multiplexing
	WLAN	Wireless Local Area Network
	WMAN	Wireless Metropolitan Area Network
	DVB-T	Digital Video Broadcasting — Terrestrial
	PAPR	Peak-to-Average Power Ratio
	SLM	Selective Mapping Technique
	PTS	Partial Transmit Sequence Technique
	UPEN	Correlation Detectors Factor
	DFT	Discrete Fourier Transforms
	FFT	Fast Fourier Transforms
	IFFT	Inverse Fast Fourier Transforms
	DSP	Digital Signal Processing
	СР	Cyclic Prefix
	S/P	Serial to Parallel
	P/S	Parallel to Serial

- Analog to Digital Convertor ADC
- High Power Amplifier HPA
- SNR Signal-to-Noise Ratio
- R Transmission Rate
- Tmc Time Multichannel
- Ν Number of sub-carrier
- Inter-sample interference ISI
- MCM Multi carrier modulation
- di **Complex Modulation Symbols**
- CCDF Complementary Cumulative Distribution Function
- BER Bit Error Rate

Pm

V

W

- AMINA Statistical Independent Sequences (route number) in SLM technique М
  - Rotation factor or weighting factor in SLM technique
- 16-QAM 4-Bits (Quadrature Amplitude Modulation)
  - Non-overlapping sub-block in PTS technique
- Weighting Factor in PTS Technique bv
  - Number of Phase Variation values in PTS Technique

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	DSP	Digital Signal Processing
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	S/P	Serial to Parallel
	P/S	Parallel to Serial

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