Design and Analysis of High Performance Reflectarray Resonant Elements

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Abstract

This paper reports on the performance comparison of different structures of reflectarray resonant elements operating in X-band frequency range. A thorough investigation has been carried out in terms of reflecting area, surface current density, reflection loss, 10% bandwidth, reflection phase and Figure of Merit (FoM). Predicted results based on Finite Integral Method (FIM) demonstrate that rectangular patch element with widest reflecting area of 105.46 mm² and surface current density of 162 A/m is shown to offer minimum reflection loss and static phase range of 0.23 dB and 120° respectively, whereas triangular loop with a smallest reflecting area of 7.46 mm² and surface current density of 3925 A/m exhibits maximum reflection loss and static phase range of 3.90 dB and 190°. Moreover it has been shown that FoM value increases with an increase in static phase range performance.

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Keywords: X-band; reflectarrays; resonant elements; surface current distribution; static phase range; figure of merit.

1. Introduction

This Reflectarrays combine best features of parabolic reflectors and phased array antennas. A microstrip reflectarray consists of a flat array of printed radiating elements on a dielectric substrate which are illuminated by a feed horn antenna. This feeding method eliminates the complexity and losses of the feeding network used in planar arrays [1]. Reflectarray antennas with advantages of low profile, low mass, flat structure and high gain are considered for direct broadcast satellite (DBS) services and applications in microspacecraft missions [2], [3]. Despite these advantages the major shortcoming of reflectarrays is the narrow bandwidth, which is primarily limited by the patch elements, differential spatial phase delay [4], [5] and the phase errors related to the change in patch size [6]. Thick substrate has been proposed in the past as a method to broaden the bandwidth which would in turn reduce the slope of phase response. Unfortunately, the smaller attainable phase range in such cases has an adverse effect on gain and overall radiation efficiency [7]. Another major issue in the design of reflectarrays is the technique required for the phase compensation of adjacent elements. The individual elements of the reflectarray are designed to scatter the incident field with proper phase required to form a planar phase surface in front of the periodic array of the aperture [7]. Variety of resonant elements can be used for reflectarray unit cells such as identical

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patches of variable-length stubs [8], square patches of variable size [9], identical planar elements of variable rotation [10], cross-dipoles [11], [12] and ring elements [13], [14]. There are two main parameters that are important in the phase compensation process, the phase range and the phase characteristics gradient. Meanwhile the phase slope oversees the manufacturing tolerances and the operational bandwidth of the element [15].

The purpose of this research work is to analyze the reflection characteristics and phase range of various reflectarray resonant elements resonating in X-band frequency range. The variation of surface current density on the conducting surface of each resonant element at resonance has been investigated to examine the effects on the reflection loss and phase range performance.

2. Unit Cell Design Considerations

In order to investigate the scattering characteristics, the case of vertically polarized (Y-axis) TEM plane wave that is normally incident on an infinite periodic array of identical elements is considered. The incident wave propagates along Z-axis, whereas the E-field of the incident energy gets polarized in Y-axis and H-field of the incident energy is polarized in X-axis [16]. TEM consideration is employed by using commercially available CST computer model to provide a good approximation for the phase range and slope.

![Design and dimensions of reflectarray resonant elements](image)

Fig. 1. Design and dimensions of reflectarray resonant elements (a) rectangular patch, (b) square patch, (c) triangular patch, (d) dipole, (e) square loop, (f) triangular loop

<table>
<thead>
<tr>
<th>Resonant Element</th>
<th>Area of Resonating Element (mm²)</th>
<th>Surface Current Density (A/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rectangular Patch</td>
<td>105.46</td>
<td>162</td>
</tr>
<tr>
<td>Square Patch</td>
<td>82.44</td>
<td>254</td>
</tr>
<tr>
<td>Triangular Patch</td>
<td>58.10</td>
<td>378</td>
</tr>
<tr>
<td>Dipole</td>
<td>19.80</td>
<td>621</td>
</tr>
<tr>
<td>Square Loop</td>
<td>11.84</td>
<td>666</td>
</tr>
<tr>
<td>Triangular Loop</td>
<td>7.46</td>
<td>3925</td>
</tr>
</tbody>
</table>

In this section, different types of resonant elements are designed and analyzed by mounting on top of 1mm thick Rogers RT/Duroid 5880 (\(\varepsilon_r=2.2\), \(\tan\delta=0.0009\)). The substrate is backed by a conducting ground plane and the copper thickness used is 0.035mm. The elements that are considered include rectangular patch, square patch, triangular patch, dipole, square loop and triangular loop. Fig. 1 illustrates the design and geometrical dimensions of each unit cell element at 10GHz whereas the area of resonant elements is calculated by mathematical formulas given in Table 1.
3. Results and Discussion

3.1. Surface Current Density

The incident TEM field generates electric current densities \( (J) \) on the conducting surfaces of the resonating elements. These fields are maximum at the resonant frequency. This is because at the resonant frequency the reflectivity of a reflectarray is at its maximum level and hence it offers higher losses \[18\]. The current distribution results generated from the commercially available computer model of CST are shown in Fig. 2. For all resonant elements it can be observed that maximum current is confined along the length of the patch at each opposite sides in vertical direction (Y-axis).

As depicted in Table I, rectangular patch with largest reflecting area of 105.46mm\(^2\) is shown to exhibit a minimum surface current density of 162A/m. The surface current is increased up to 3925A/m when triangular loop with reflecting area of 7.41mm\(^2\) is made to operate at the same frequency. This high concentration of surface current distributions in triangular loop is due to the fact that reduction in the geometrical dimensions enables the current to flow the long path along the curvature of the loop, hence offers the highest value of current density among all resonant elements. Thus, it can be concluded that reduction in the resonating area of the patch elements tends to increase the surface current density \( (J) \) and amount of current \( (I) \) according to the Maxwell’s equation \[18\].

\[
I = \int J \, ds \tag{1}
\]

Also \( (J) \) is related with the incident electric field \( (E) \) as represented by the following equation.

\[
J = \sigma E \tag{2}
\]

Where \( \sigma \) is the electrical conductivity of the material.

Fig. 2. Surface current density on reflectarray resonant elements; (a) rectangular patch, (b) square patch, (c) triangular patch, (d) dipole, (e) square loop, (f) triangular loop
3.2. Reflection Loss and 10% Bandwidth Performance

Reflection loss is considered to be an important parameter in the analysis of loss performance of reflectarrays. Fig. 3 shows the reflection loss curves of different resonating elements. It is illustrated in Fig. 3 that rectangular patch element is observed to offer the lowest reflection loss value of 0.23dB whereas triangular loop gives the highest reflection loss value of 3.90dB. This is significantly due to the fact that surface area of the triangular loop is very small as compared to rectangular patch element, which allows more current distribution to be concentrated in the central region of the length of the loop.

Table 2. Reflection Loss and 10% Bandwidth

<table>
<thead>
<tr>
<th>Resonant Element</th>
<th>Reflection Loss (dB)</th>
<th>10% Bandwidth (MHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rectangular Patch</td>
<td>0.23</td>
<td>388</td>
</tr>
<tr>
<td>Square Patch</td>
<td>0.28</td>
<td>272</td>
</tr>
<tr>
<td>Triangular Patch</td>
<td>0.36</td>
<td>240</td>
</tr>
<tr>
<td>Dipole</td>
<td>0.76</td>
<td>124</td>
</tr>
<tr>
<td>Square Loop</td>
<td>1.49</td>
<td>84</td>
</tr>
<tr>
<td>Triangular Loop</td>
<td>3.90</td>
<td>76</td>
</tr>
</tbody>
</table>

The bandwidth of reflectarray cell elements can be calculated by the reflection loss curves. In order to analyze the bandwidth performance, the bandwidth is defined by moving 10% above the maximum reflection loss value [19]. Table 2 contains the 10% bandwidth of all the investigated resonant elements. It can be seen from Table 2, that rectangular patch gives a wider bandwidth of 388MHz as compared to triangular loop element which gives minimum bandwidth of 76MHz.
The results demonstrate that resonant elements with the highest surface current density are shown to give higher reflection loss whereas resonant elements with the lowest surface current density are observed to give broader bandwidth performance.

Fig. 4 shows the effect of reflective area of resonant elements on the reflection loss and surface current density. It can be seen that as the area reduces from 105.46mm² to 7.46mm², the reflection loss and surface current density increase from 0.23dB to 3.90dB and 162A/m to 3925A/m respectively. This is because the reflectarray resonant element with smallest area of resonance dissipates more energy into the substrate region which results in an increased surface current density and reflection loss value.

3.3. Reflection Phase and Figure of Merit (FoM)

Reflection phase is another important parameter that is used to analyze the reflectivity and bandwidth of reflectarrays. Moreover phase errors can also be observed using phase plots. The reflection phase curves for all the resonant elements are presented in Fig. 5. It can be observed form Fig. 5 that rectangular patch element acquire smoother phase characteristics gradient as compared to triangular loop, which is shown to exhibit the steepest phase characteristics gradient among all resonant elements. Since the overall phase variation is smaller than 360° therefore the maximum phase range can be obtained at the expense of steep slope, alternatively a smooth slope can be obtained at the expense of reduced phase range.

![Fig. 5. Reflection phase curves of different resonant elements](image)

The comparison of reflection phase performance can be indicated by Figure of Merit (FoM) and static phase range. FoM can be defined as the change in the reflection phase to the change in frequency and can be expressed as [20].

\[ FOM = \frac{\Delta \phi}{\Delta f} \left(\frac{\circ}{\text{MHz}}\right) \]  

(3)

Static phase range and FoM values of various reflectarray resonant elements are depicted in Table III. It can be observed that rectangular patch element with minimum FoM value of 0.19°/MHz offers a minimum static phase range of 120° whereas triangular loop with maximum FoM value of 0.80°/MHz shows maximum static phase range of 190°. It can be seen that the static phase range performance is directly proportional to FoM.

Fig. 6 shows the relationship between bandwidth and static phase range performance. With an increase in surface current density of the resonant elements from 162 A/m to 3925A/m, the 10% bandwidth is shown to be decreased from 388MHz to 76MHz whereas static phase range is observed to increase from 120° to 190°. It can be seen that FoM is directly proportional to the static phase range and there prevails a tradeoff between bandwidth and static phase range performance.
Table 3. Static Phase Range and Figure of Merit (FoM)

<table>
<thead>
<tr>
<th>Resonant Element</th>
<th>Static Phase Range (°)</th>
<th>Figure of Merit (FoM) (°/MHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rectangular patch</td>
<td>120</td>
<td>0.19</td>
</tr>
<tr>
<td>Square patch</td>
<td>130</td>
<td>0.23</td>
</tr>
<tr>
<td>Triangular patch</td>
<td>140</td>
<td>0.27</td>
</tr>
<tr>
<td>Dipole</td>
<td>155</td>
<td>0.28</td>
</tr>
<tr>
<td>Square loop</td>
<td>170</td>
<td>0.72</td>
</tr>
<tr>
<td>Triangular loop</td>
<td>190</td>
<td>0.80</td>
</tr>
</tbody>
</table>

Fig. 6. Relationship between bandwidth and static phase range with variation in surface current density

4. Conclusion

Different unit cell elements have been analyzed for the performance optimization of reflect arrays. It has been shown that a reduction in reflecting area of the resonant elements modifies the electrical dimensions and surface current density which can significantly affect the reflection loss and reflection phase performance. Triangular loop is shown to offer greater static phase range as compared to other elements. It is shown that by employing triangular loop as reflect array resonant element the feasibility to enhance the static phase range can be realized. However the increase in the static phase range has to be traded-off with the bandwidth performance of reflect arrays.

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References


