SPECIFICATION OF VERTICAL SEMANTIC CONSISTENCY RULES OF UML CLASS DIAGRAM REFINEMENT USING LOGICAL APPROACH

NURAINI ABDULGANIYYI

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Faculty of Computer Science and Information Technology
Universiti Tun Hussein Onn Malaysia

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ABSTRACT

Unified Modelling Language (UML) is the most popular modelling language use for software design in software development industries with a class diagram being the most frequently use diagram. Despite the popularity of UML, it is being affected by inconsistency problems of its diagrams at the same or different abstraction levels. Inconsistency in UML is mostly caused by existence of various views on the same system and sometimes leads to potentially conflicting system specifications. In general, syntactic consistency can be automatically checked and therefore is supported by current UML Computer-aided Software Engineering (CASE) tools. Semantic consistency problems, unlike syntactic consistency problems, there exists no specific method for specifying semantic consistency rules and constraints. Therefore, this research has specified twenty-four abstraction rules of class’s relation semantic among any three related classes of a refined class diagram to semantically equivalent relations of two of the classes using a logical approach. This research has also formalized three vertical semantic consistency rules of a class diagram refinement identified by previous researchers using a logical approach and a set of formalized abstraction rules. The results were successfully evaluated using hotel management system and passenger list system case studies and were found to be reliable and efficient.
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<td>UML</td>
<td>Unified Modelling Language</td>
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<td>IT</td>
<td>Information Technology</td>
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<td>OMG</td>
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<td>CASE</td>
<td>Computer Aided Software Engineering</td>
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<td>Software Requirement Document</td>
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<td>SRS</td>
<td>Software Requirement Specification</td>
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<td>OOD</td>
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D - Dependency
G - Generalization
A - Bidirectional Aggregation
$\overline{A}$ - Unidirectional Aggregation
S - Association
CL - Class
Attr - Attribute
Opr - Operation
CRule - Cardinality abstraction Rule
CDRR - Vertical Semantic Consistency Rule of Class Diagram Refinement
CHAPTER 1

INTRODUCTION

The increasing dependency on computers and software applications for saving lives, properties and time, in our contemporary world has escalated to all sectors of human endeavours. Thereby, led to an increase in the demand of efficiency and reliability of the computers and the software applications before usage, to avoid claims of what they were provided to save (that is: lives, properties and time). To ensure efficiency and reliability of software applications, software experts have agreed to define the best practice for software development, namely software engineering. The discipline of software engineering is coined to deal with poor quality of software, get projects exceeding time and budget under control. It also ensures that software is built systematically, rigorously, measurably, and within specification. In other words, software engineering is the study and application of engineering to the design, development, and maintenance of software from the start to the end of the development (Laplante, 2007).

In the design phase of software engineering process, Unified Modelling Language (UML) is one of the modelling languages use for designing software project. In addition, UML has become an industrially accepted standard for object-oriented modelling of large, complex systems as well as a basis for software development methodologies (Lucas et al., 2009). This research is aimed at addressing the inconsistencies of software at the design stage. Design plays a central role in the activities that leads to the development or maintenance of good software by giving an abstract representation of the system prior to development or maintenance. The consistency of the developed or maintained system with the user
requirement specifications depends mostly on the consistency of the design. According to Ralph & Wand (2009), software design (the second phase of software development life cycle (SDLC) in Figure 1.1) is the process of realizing software solution to one or more set of problems.

![Figure 1.1: Phases in SDLC (Justin, 2013)](image)

The largest segment of design phase of software development life cycle is creating a consistent design based on a comprehensive model. These days, the infrastructures for creating this design are usually based on object-oriented modelling languages. Unified Modelling Language (UML) is the most popular object-oriented modelling language used to model a system in a way that the status of the various objects replicate the user’s point of view or specification (Gogolla & Richters, 2002). The modelling task focuses on definitions and descriptions of objects, features and actions to be operated by the user during interaction, rather than on the programming aspect (Winograd, 1995).

In the early nineties, there were many graphical notations invented for object-oriented software modelling, not until 1995 when Grady Booch and Jim Rumbaugh’s concepts were combined and named as unified method. When Ivar Jacobson joined Booch and Rumbaugh the unified method was later called Unified Modelling Language (UML). The three are since then called the “Three Amigos” in the world
of software engineering and information technology (IT) (Weilkiens & Oestereich, 2010). There are seventeen types of diagrams in UML 2.5 (Ciancarini, 2013 & Ambler, 2013).

As UML is used to model system from different viewpoints and abstraction levels, consistency issues need to be taken into consideration as diagrams representing various aspects of the system are produced. Inconsistency occurs when the diagrams are not properly related to each other in order to form a reliable description of the user requirement specifications (Lucas et al., 2009). The benefit of checking consistency of a UML model at design stage shall never be over emphasized as quality assurance technique. It often results in better design; earlier detection of errors, flaws, product delivery within budget and time scheduled. Moreover, consistent model makes system maintenance, and team works easier even at different geographic location (Nugroho & Chaudron 2009, Usman et al., 2008).

There are two types of inconsistency problems: vertical and horizontal consistency problems. Those related to models constructed at the same level of modelling abstraction are called intra-consistency or horizontal consistency problems. While those between models built at different levels of abstraction i.e. between a model and its successive refinement are called inter-consistency or vertical consistency problems (Huzar et al., 2005). Inconsistency problems occur in a UML model due to multi-view nature of the UML diagrams and iterative process of information system development. Other possible sources of inconsistency in UML include; imprecise semantic nature of the UML diagrams and distributed development of a system with several developers. The developers may on occasions, be geographically distributed locally or globally, with various interpretations of both the requirements and the UML notations (Huzar et al., 2005).

Furthermore, Lucas et al., (2009) classified previous works on consistency management into syntactic and semantic consistency problems. They also suggested the use of formal approach to solve inconsistency problems in a way that will improve feedback of the consistency check with aim of easing modellers’ task of identifying and handling problem(s) detected in a model. Therefore, this dissertation aims at formalizing class diagram elements and vertical semantic consistency rules of class diagram refinement using a logical approach. This technique will benefit from the properties of mathematical logic such as transitivity, associativity and
1.1 Problem Statement

Despite the popularity of UML for object-oriented software modeling in software development industries, UML diagrams are being affected by inconsistency problems at the same and different modeling abstractions. Inconsistency problems of UML diagrams are the major setback recorded affecting modeling with UML. Solving UML inconsistencies have gained the attention of many researchers on how to handle inconsistency in UML, though there are limited works in UML vertical semantic inconsistency management (Lucas et al. 2009, Torre & Genero 2014). In general, syntactic consistency problems can be automatically checked and, therefore, are supported by current UML CASE tools (Khalil & Dingel 2013). Unlike syntactic consistency, there is no specific method for specifying semantic consistency rules and constraints (Khalil et al. 2013). Shen, Wang, & Egyed (2009) identified three vertical semantic consistency rules of a class diagram refinement and used informal approaches to manage them. The approaches used were Integrated Abstraction and Comparison (IAC), and Separated Abstraction and Comparison (SAC). These techniques require a significant amount of time and memory space in order to handle inconsistencies of a class diagram refinement. These are due to the large number of rules check and iterations involved in the algorithms. On the contrary, this research will formulate the same vertical semantic consistency rules of class diagram refinement achieved with SAC and IAC in a more effective and efficient manner using a logical approach.

1.2 Aim and Objectives of the Research

This research aims to formalize class diagram elements and vertical semantic consistency rules of class diagram refinement using logical approach.
The objectives of the research are to:

(i) identify UML class diagram elements for vertical semantic consistency of class diagram refinement.
(ii) produce a formal specification for the three rules identified by Shen et al., (2009).
(iii) validate (ii) using hotel management system and passenger list system case studies.

1.3 Significance of the Study

Modelling a software system with UML helps to improve productivity and quality of the software product by ensuring that all stakeholders understand the target system in a single way. Consequently reduces the defect density in the code and the time required to fix the defects (Nugroho & Chaudron 2013). However, these advantages are often challenged by inconsistency of the UML diagrams. Therefore, there is a need to check consistency of the UML models at design stage to obtain better design, detect errors and flaws at the early stage of development. Moreover, consistent design facilitates product delivery within budget, time scheduled, and make teamwork comfortable even at different geographic locations (Nugroho & Chaudron 2009, Usman et al., 2008). Hence, formalizing class diagram elements and vertical semantic consistency rules of class diagram refinement will reduce the ambiguity of UML CASE tool support for vertical semantic inconsistency management of class diagram refinement (Shen et al., 2009).

1.4 Scope of the Study

This study will be restricted to formalization of class diagram elements and three vertical semantic consistency rules of class diagram refinement identified by Shen et al., (2009) using a logical approach. The results will be validated using hotel management system and passenger list system case studies.
1.5 Report Organization

This dissertation is organized as follows: Chapter 2 is the literature review of the research. It presents a general discussion of the major aspects of the study. It begins by explaining object-oriented software development life cycle, object-oriented analysis, and object-oriented design. It further discusses UML for object-oriented software design and inconsistencies in UML. The chapter then discusses the related works to the study. Chapter 3 discusses the methodology of the research. It presents an explanation of three vertical semantic consistency rules of class diagram refinement, definition of logic and set, logic and set symbol and finally gives explanation and sketch of the research framework. Chapter 4 will formalize the vertical semantic consistency rules of class diagram refinement. It presents a formalization of class diagram elements, class diagram abstraction rules and finally presents formalization of the three vertical semantic consistency rules of class diagram refinement. Chapter 5 will evaluate the formalized rules with a case study. It presents a case study of hotel management system to evaluate the formalized rules. Finally, Chapter 6 presents conclusion of the research and outlines some future works.
CHAPTER 2

LITERATURE REVIEW

This chapter discusses literature related to this research in order to establish facts about the problem this study addresses. Section 2.1 and its subsections explain one of the methodologies of developing quality software in the present state of technology. Section 2.2 gives a brief history and explanation of Unified Modelling Language (UML), and Section 2.3 reviews previous works related to this study.

2.1 Object Oriented Systems Development Life Cycle

Object-Oriented Systems Development Life Cycle (OOSDLC) is a process of developing high-quality software that meets both customer and actual world requirements. OOSDLC consists of three primary processes: Object-oriented analysis, Object-oriented design, and Object-oriented implementation. These processes are seen as a sequence of alteration, where output of one transformation becomes input for subsequent transformation. Fundamentally, product of object-oriented analysis is input to object-oriented design; product of object-oriented design is input to object-oriented implementation of the intended system using object-oriented programming techniques (Booch, 2007).
2.1.1 Object Oriented Analysis

Object-Oriented Analysis (OOA) is a process of analysis that scrutinizes client’s requirements from a viewpoint of classes, objects and relationship among them, as contained in the vocabulary of the problem domain (Booch, 2007). The result of this analysis includes both functional and non-functional requirements that are document in a Software Requirement Document (SRD). SRD contains Software Requirement Specification (SRS) which presents the result of the functional requirement analysis using Unified Modelling Language (UML) diagrams. SRS is used to set basis for agreement between a developer and a client on what the software product is to do as well as what it is not expected to do. Moreover, SRS allows a thorough evaluation of requirements before design can commence and thus reducing the chances of redesigning. SRS can also serve as a reasonable basis for estimating a product cost, risks and schedules (McConnell, 2010).

There are many proven methods for analysis of an object-oriented system to get various classes and objects from elements of the problem domain. These methods include classical, behaviour, domain, use case, CRC cards, informal English description, and structured analysis method (Booch, 2007). For instance, to analyze a system using the classical analysis method, Shlaer & Mellor (1988) proposed that candidate classes and objects, should regularly come from one of the following sources. First, tangible objects such as bicycle, washing machine, telemetry data, pressure sensors among others. Second, role model such as farmer, engineer, and doctor. Third, events like landing, packaging, malting, interrupting and requesting. Fourth, interactions like loan, withdrawal, meeting, and intersection (Booch, 2007).

Moreover, Coad & Yourdon (1991) proposed other sources of potential objects as follows. First, structures like "Is a" and "part of" relationships. Second, other external systems with which an application interacts. Third, devices an application interacts with. Fourth, events that must be recorded. Fifth, roles play by users in interacting with an application. Sixth, any physical location which is critical to an application such as classroom, university and hospital. Lastly, organizational units to which an application users belong. The results obtained from any of the chosen analysis approaches are modelled using UML and documented in the SRS, which serves as input to the object-oriented design phase (Booch, 2007).
Consequently, this research will present formalization of vertical semantic consistency rules of class diagram refinement. The formalized rules will be used to check consistency of a class diagram at object-oriented design phase with a class diagram obtained at object-oriented analysis phase of software development.

2.1.2 Object-Oriented Design

Object-oriented design (OOD) is a technique of design that deals with object-oriented breakdown and a notation for representing both logical and physical as well as static and dynamic aspect of the system under design (Booch, 2007). OOD uses class and object concepts to structure a system logically while structural design uses algorithmic concepts. The objective of OOD is to design classes (identified during the analysis phase), graphical user interface classes and add other classes that will breakdown or refine the classes obtained in the analysis phase. Furthermore, during this phase, other objects and classes that will support implementation of the user’s requirements, may also be identified and defined, such as classes for connection to the database (Booch, 2007). Consequently, produces a technical description of how solution to client’s requirements and expectations can be achieved using the various diagrams of UML. The following section gives details information on UML, definition, and notations of a class diagram.

2.2 Unified Modelling Language

The Unified Modelling Language (UML) is a language and notation system use to specify, construct, visualize, and document models of software systems (OMG, 2005). It provides sets of diagrams to model structural, behavioural, and interaction aspects of an object-oriented system. Each diagram depicts a particular design aspect of the system. UML consists of many diagrams depending on the version. For example, UML version 2.0 has 13 diagrams (OMG, 2005), both UML version 2.2 and 2.4 have 14 diagrams (Zhao, et al., 2011) and UML version 2.5 has 17 diagrams (Ambler, 2013). These 17 diagrams are divided into three categories. The first category contains ten diagrams use to represent static structures of an application and
are called structure diagrams. These include class, object, component, composite structure, package, deployment, profile, model, manifestation, and network architecture diagram. The second category comprises of three diagrams used to represent general types of behaviours in a software application and are referred to as behaviour diagrams. Behaviour diagrams include use case, activity and state machine diagram. The last category contains four diagrams representing different aspects of interactions of the system under development and is called interaction diagrams. The diagrams in this category are all derived from the more general behaviour diagrams. Interaction diagrams include sequence, communication, timing, and interaction overview diagram. The presence of many UML diagrams, to model a system, brings a variety of views that overlap with respect to information depicted in each that can leave overall system design specification in an inconsistent state.

### 2.2.1 UML Model Consistency

Consistency in UML model is a state in which the structures, features and elements that appear in a model are compatible and in alignment with contents of the model and other related models with respect to requirement being modeled and UML metamodel (Spanoudakis & Zisman, 2001). For example, the structures, functions and relations in an initial class diagram obtained during an analysis phase of a software development must be compatible with a detailed class diagram developed during the design phase of the software development.

In addition, unambiguous and consistent UML models are necessary for successful development of quality Information System (IS) (Bansiya & Davis, 2002). However, UML model is hardly free of inconsistency problems within or with other models at the same or different abstraction levels. Inconsistency in UML model(s) usually arose due to analysts or designers viewing the same system from different points of views. Other possible causes of UML inconsistency are iterative process of an IS development, lack of UML knowledge or practice, imprecise semantic nature of the UML diagrams, difference in geographical location of developers, and multiple interpretations of user’s requirements and UML notations (Huzar et al., 2005).
Iterative process of an IS development involves UML diagrams abstraction. Abstraction is the process of creating decomposition of a diagram into simpler and better understood primitive diagrams. This procedure has many underlying methodologies. An abstraction can also be used to refer to a model (Burback, 1998). The process of transforming one abstraction into a more comprehensive abstraction is called refinement. The abstracted diagram is referred to as a refinement of the original one (Burback, 1998). Abstractions and its refinements naturally do not coexist in the same system description. Accurately, what is meant by a more comprehensive abstraction is not well defined. Therefore, there is a need to support substitutability of concepts from one abstraction to another (Burback, 1998).

Furthermore, consistency checking must be performed within and between different UML models to reduce the cost, time, and effort of maintenance (Dam & Winikoff, 2010). This is principally true in the context of design evolution. There are two types of consistency problems in UML; vertical and horizontal. Vertical and horizontal consistency problems are also classified into syntactic and semantic consistency problems. The definitions of the types and classifications of consistencies are described as follows.

(i) Vertical Consistency

Vertical consistency in UML is a state of semantic or syntactic compatibility of models built at different levels of abstraction such as between a model and its refinement. It is also called inter-consistency (Huzar et al., 2005). For example, an abstract class diagram developed in the analysis phase of software development must be semantically and syntactically consistent with a detailed class diagram developed in the design phase of the software development.

(ii) Horizontal Consistency

Horizontal consistency is a state of semantic or syntactic compatibility of models built at the same level of modelling abstractions. It is also called intra-consistency (Huzar et al., 2005). For example, a class diagram describing the static aspects of an abstract model must be semantically and syntactically consistent with a state machine diagram describing the dynamic aspects of the classes in the model.
(iii) Semantic Consistency

Semantic consistency is a state that requires models’ behaviours to be semantically compatible with one another (Engels, et al., 2001). For example, a class diagram and its refinement must be semantically compatible with each other. Unlike syntactic consistency, there is no specific method for specifying semantic consistency rules and constraints (Khalil & Dingel, 2013).

(iv) Syntactic Consistency

Syntactic consistency guarantees that a model conforms to abstract syntax of the modelling language as specified by its meta-model (Engels et al., 2001). For example, in a class diagram, the design of each class as well as the relationship between them must be syntactically correct in accordance with the class diagram meta-model. In general, syntactic consistency can be automatically checked and therefore is supported by current UML CASE tools (Khalil & Dingel, 2013).

The inconsistency type depends on whether the inconsistency issue is due to violation of rule(s) of UML meta-model or compatibility of UML diagrams used in the modelled system (Engels, Küster, et al., 2001, Lucas et al., 2009). Despite all the challenges of consistency uncertainty of UML models, UML is also the most widely used modelling language in object-oriented software development industries. Class diagram is the most used UML diagram (Dobing & Parsons, 2006). For this reason, this research will propose a formal specification for three vertical semantic consistency rules of class diagram refinement identified by Shen et al., (2009) using a logical approach. The following section will dwell on a class diagram and its properties.

2.2.2 Class Diagram

A class diagram is the most fundamental and broadly used UML diagram. It illustrates the static view of a system, consisting of classes, their interrelationships, operations and attributes of the classes (Szlenk, 2006). A Class is the building blocks of an object-orientated system. It is used to depict the static view of a system or part
of the system, describing its attributes and methods (operations) without detailing how to achieve the methods. A class in UML is represented by a rectangle showing the name of the class and optionally names of methods and attributes. Partitions are used to divide the class name, attributes and operations. The top partition of a class contains the class name, the second partition contains attributes of the class, and the third partition contains operations in the class and their parameters if any. The notation that precedes the attribute’s or method’s name indicates the visibility of the element. If “+” (plus) symbol is used, the attribute or method, has a public level of visibility. If “–”(minus) symbol is used, the attribute or method, is private. Furthermore, “#” symbol allows a method or attribute, to be defined as protected while “~” symbol indicates package visibility (Weilkiens & Oestereich, 2010). Figure 2.1 shows an example of class, named Rectangle.

![Class Diagram Example](image)

**Figure 2.1:** Example of a class (Coates, 2012).

Furthermore, a class diagram illustrates relationships between classes and interfaces. Generalizations, aggregations, and associations are all precious in reflecting inheritance, composition or usage, and connections, respectively between classes (Weilkiens & Oestereich, 2010). A generalization is an abstraction principle use to organize semantics of a model hierarchically. It shows the relationship between a general class and a particular class. The particular class posses all the characteristics of the general class, and other special features and behaves in a way well-suited to the general class. An association expresses a tuple of typed instances. It is represented by a straight line, and at least two properties take part in the association. Multiplicity of an association states how many objects of the associated
classes can participate in the association. If this number is a variable, a range is stated that is, the minimum and maximum value. A minimum of “0” means that the relationship is optional: the relationship exists, but the number of elements involved in the association may be 0. Dependency is used to describe dependency between two elements of a system. An aggregation is an association extended by a semantically noncommittal comment that participating classes have no equal-ranking relationship. Instead, they represent a whole-parts hierarchy. An aggregation is used to illustrate how something whole is logically composed of its parts. A composition is a strict form of aggregation, where the existence of its parts depends on the whole. The whole is the owner of its parts. The composition also describes how something whole is composed of individual parts (Szlenk, 2006). Figure 2.2 shows elements of a class diagram and Figure 2.3 shows how a class relates with others to build a class diagram using some of the class diagram elements of Figure 2.2. This research will formulate vertical semantic consistency rules of a class diagram refinement with respect to the class diagram elements of Figure 2.2 using logical approach. Class diagram and class model are often interchangeably used to refer to the same thing. The following subsection explains refinement.

Figure 2.2: Elements of Class Diagram
2.3 Refinement

Refinement is a procedure of transforming a model into a more comprehensive model. The new model is referred to as a refinement of the original model (Burback, 1998). According to Hnatkowska et al., (2004), refinement is a relationship that represents a more detailed specification of something that has previously been specified at a certain level of detail. For example, a design phase class diagram is a refinement of the analysis phase class diagram. Models and their refinements naturally do not coexist in the same system description. Precisely, what is meant by a more comprehensive model is not well defined. Thus, there is a need to get support for substitutability of concepts from one model to another (Burback, 1998).

Moreover, relationships between elements in different models have no semantic impact on the contents of the models because of the self-containment of the models. However, they are useful for tracing refinements and for keeping track of requirements between models (Hnatkowska et al., 2004).
2.4 Formalization

This research will use a logical approach to formalize vertical semantic consistency rules of class diagram refinement. In mathematics, the study of logic deals with statements or propositions. A statement is a sentence that is either true or false, but not both. For example, it rained yesterday. Logical investigation conveys clearly the required relationships between facts about the real world and show where possibly unwarranted assumptions enter into them. Mathematically, logic is referred to as a tool for working with complex compound statements which involves using formal language for expressing them, concise notation for writing them and a methodology for objectively reasoning about their truth or falsity. Also, logic is the basis for stating formal proofs in all branches of mathematics (Shoenfield, 1967).

Set theory is a natural extension of logic and provides further useful notation as well as some interesting insights of its own. Set is a well-defined collection of objects. Even though any object can be collected into a set, set theory is applied most often to objects that are relevant to mathematics. The language of set theory can be used in the definitions of nearly all mathematical objects (Stoll, 2012). This research will identify elements of a class diagram and formalized it using set theory. The formal definition of class diagram will then be used to logically formalize abstraction rules and cardinality semantics of class’s relations. Finally, the formalized definition of class diagram, abstraction rules and cardinality semantics of class’s relation will be used to formally specify three vertical semantic consistency rules of class diagram refinement.

Besides, logical approach has been considered sufficient for checking and managing inconsistency in UML diagrams. Lucas et al. (2009) found that 75% of the techniques used in 44 proposals from 2001 to 2007 for detecting and handling inconsistency problems were formal methods and 21% of the procedures were logical approach. The authors concluded that this high percentage disclosed, that use of formal methods, offer advantages in dealing with consistency problems, even though none of the formal methods used standout above the others. The authors thereby recommended using a formal technique to handle inconsistency problems of UML diagrams in future works.
2.5 Review of Previous Works

Although there are many proposals for enhancing modelling with UML, only a few works on UML semantic consistency management (Lucas et al., 2009; Torre & Genero, 2014). While some of the proposals used formal methods to enhance UML modelling and software development process, others used informal methods. Lima et al., (2009) proposed a formal verification and validation (V&V) technique to check semantic consistency of a sequence diagram. The proposed technique generate PROMELA-based model from interactions expressed in a given sequence diagram. SPIN model checker is then used to simulate the execution and to confirm sequence diagram properties are written in Linear Temporal Logic (LTL). The technique was implemented as an Eclipse plug-in, with human understandable feedback to the developer. The following semantic rules of a sequence diagram were addressed; lifeline that performed the last action, the last completed action (sent or received), message used in the final action, and lifeline to/from which a message was sent/received. This technique is difficult to extend to static components of UML diagrams. According to Holzmann & Gerard (2007), PROMELA is a process modelling language which intended use is to verify the logic of parallel systems. In other words, PROMELA can be highly suitable for modelling dynamic properties but not static features.

Shen, Wang, & Egyed (2009) presented two informal methods for checking consistency between a class diagram and its refinement at different levels of modelling abstractions. The presented techniques were Integrated Abstraction and Comparison (IAC), and Separated Abstraction and Comparison (SAC). The authors further demonstrated that SAC is highly favourable for consistency checking of software models than IAC. The techniques addressed three semantic consistency rules of class diagram refinement. The addressed rules are stated as follows; (1) every low-level class refines at most one high-level class, (2) every high-level class has at least one low-level class, which refines the high-level class, and (3) the group of relationships between any two high-level classes must be identical with the group of relationships between their corresponding low-level classes. The methods were implemented and integrated with IBM Rational Rose design tool.
He et al. (2013) proposed a method of ontology-based semantics confirmation of UML behaviour diagrams. The authors divided semantics of behaviour diagrams into static and dynamic semantics. The static semantics are defined as the notations and constraints in UML behavioural diagrams while the dynamic semantics are defined as the semantic relations among the instances of the notations while interacting. The static semantics of behavioural diagrams are transformed into ontology web language description logic (OWL DL) by converting UML behaviour diagrams and their meta-models into a DL knowledge base. While the dynamic semantics are specified in DL-Safe rules that are then expressed by SWRL (Semantic Web Rule Language) and added to the OWL DL ontology. The OWL DL is then used to check both vertical and horizontal semantic consistency of activity, sequence, and state diagrams.

Knapp, Mossakowski, & Roggenbach (2014) proposed a technique called institution based heterogeneous approach for checking semantic consistency among UML diagrams. The proposed framework can be used to verify consistency of different UML diagrams both horizontally and vertically. The vertical semantic consistency addressed in the proposal checks whether the state machine satisfies an OCL invariant or an OCL pre-/post-condition.

However, there are still issues with UML consistency checking and management, due to ambiguity of some of the proposed rules, unconformity to meta-model of the UML diagram(s), in-extensibility of some of the techniques, sometimes meaningless consistency rules proposals as well as impractical applicability of the proposed rules (Lucas et al., 2009). Table 2.1 summarises the previous works on semantic consistency in UML diagrams.
In addition, most of the previous studies were on horizontal consistency management. Lucas et al., (2009), in their systematic literature review of 44 papers from 2001 to 2007 on UML model consistency management found out that 53.13% of the 44 proposals were on horizontal syntactic and semantic inconsistency management. Whereas 18.75% of the 44 studies were on vertical syntactic, and 15.63% of the 44 studies were on vertical semantic inconsistency management. Torre & Genero (2014), in their systematic mapping study of 94 papers from 2000 to 2012 also found that 98.07% of the 94 proposals were on horizontal consistency management and 1.93% of the 94 publications were on UML vertical inconsistency management.

The given reviews show that UML vertical inconsistency management has received less attention by researchers in the past. Thereby, posing the existing CASE tools for modelling UML with unsatisfactory support for its maintenance. This dissertation will formalize class diagram elements and vertical semantic consistency rules of class diagram refinement using a logical approach.
2.4 Chapter Summary

This chapter has reviewed object-oriented system development life cycle, object-oriented analysis and object-oriented design and their relationship to this study. This chapter further discussed Unified Modelling Language (UML), consistency in UML, types of consistencies, classification of consistencies, class diagram and finally reviewed previous works related to the study. The next chapter presents a methodology of this research.
CHAPTER 3

RESEARCH METHODOLOGY

This chapter explains the systematic methodology of this research in order to check inconsistency problems between two-class diagrams at different levels of abstractions. Further, this study will use elementary set theory and logic to check the inconsistency problems. Section 3.1 will state the rules to be addressed by the research. Section 3.2 will define and give examples of set symbols and logical terms that will be used to formalize a class diagram and check the rules stated in Section 3.1. Section 3.3 presents a framework of how the formalization will be used to check inconsistency between class diagrams at different levels of abstractions. The last Section 3.4 will present summary of the chapter.

3.1 Vertical Semantic Consistency Rules of Class Diagram Refinement

This section discusses three (3) vertical semantic consistency rules of a class diagram refinement identified by Shen et al., (2009). Refinement occurs when an initial class diagram obtained during the analysis phase of a software development is broken-down to a detailed class diagram during design phase of the software development. This research shall refer to the initial class diagram obtained at analysis phase as high-level class diagram and detailed class diagram obtained at design phase as low-level class diagram.
According to Shen et al., (2009), two-class diagrams at different levels of abstractions are said to be consistent with each other if the following consistency rules (CDRR) are satisfied:

(i) **CDRR1**: Every class of a low-level class diagram (LCD) refines at most one class of the high-level class diagram (HCD): ensures that a low-level class refines at most one high-level class. This means that a low-level class can be a subclass of at most one high-level class: specialization.

Refinement is a procedure of transforming one class into simpler and more understood primitive classes (Burback, 1998). Specialization means creating new subclasses from an existing class. Generalization is a process of extracting shared characteristics from two or more classes and combining them into a generalized super class. Shared characteristics can be attributes, associations, or methods.

Figure 3.1 explains CDRR1 using a high-level class diagram and a low-level class diagram. The high-level class diagram consists of three classes; A, B and C. The low-level class diagram consists of all classes in the high-level class diagram probably with additional properties or attributes (i.e. class A´, B´ and C´). The low-level class diagram also contained class D and E. Applying CDRR1 to Figure 3.1 reveals that: the low-level class diagram is a wrong refinement of the high-class diagram due to class E refining two classes that are part of the high-level class diagram, thereby violating CDRR1.

Another example of CDRR1 is shown in Figure 3.2 which consists of a high-level class diagram and a low-level class diagram. The high-level class diagram consists of three classes A, B and C. The low-level class diagram consists of all classes in the high-level class diagram with perhaps additional properties or attributes (i.e. class A´, B´ and C´) and additional two classes, D and E. The low-level class diagram is a successive refinement of the high-level class diagram with class D specializing class A, and class E generalizing classes B and C.
Figure 3.1: Wrong class Diagram refinement violating CDRRI

Figure 3.2: Successive Class Diagram Refinement in line with CDRRI
(ii) **CDRR2**: Every high-level class has at least one low-level class, which refines it: ensures that every high-level class is refined or present in the low-level class diagram since a class is a refinement of itself. In another world, every high-level class must be present in the low-level class diagram with either further refinement or no refinement.

*CDRR2* is illustrated in Figure 3.3 and 3.4. The low-level class diagram of Figure 3.3 consists of class A, B, C and D and the high-level class diagram consists of class A’, B’, C’, E, F, G, H, I, and J. Class D of the high-level class diagram is missing in the low-level class diagram and that violate *CDRR2* because class D does not refine itself nor another class in the low-level class diagram. Moreover, class F and J refined or specialized class A, class E refined or specialized class B, and lastly class G, H and I refined class C.

Figure 3.4 consists of high-level class diagram and low-level class diagram. The high-level consists of class A, B, C and D while the low-level class diagram consists of class A’, B’, C’, D’, E, F, G, H, I, and J. The low-level class diagram is a successive refinement of the high-level class diagram. Class G, H and I refined or specialized class D, class E generalized class C, class F and J refined or specialized class B and finally the class A refined itself.
REFERENCES


