REYNOLDS NUMBER EFFECTS IN DESIGNING A MICROMIXER FOR BIOMEMS APPLICATION

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A project report submitted as a partial fulfillment of the requirement for the award of the Master's Degree in Electrical Engineering

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NOVEMBER, 2008

ACKNOWLEDGEMENT

I wish to thank and acknowledge the assistance and contributions of several people without whom this project would not be possible.

First and foremost, I would like to express my sincere appreciations to my supervisor, Dr Muhammad Mahadi bin Abdul Jamil who provides his invaluable guidance for the work throughout my project. Many thanks to him for his frequent discussions with me about my general research directions and technical details which not only expanded my horizons but also stimulated my creativity and imagination. Thanks also due to my co-supervisor, Mr Alabqari bin Ma'Radzi, for his advice. Our meetings were a tremendous help and he provided assistance in every aspect of my work, above and beyond his duties. Thanks to the other postgraduates who are always there to listen to me when I needed someone to talk to or to help me with alternative views. Thank you very much for your friendship and I cherish the moments we shared together very much!

Finally I wish to thank my dear husband, Kusiar bin Wagimen, for his confidence in my capability, who pushes me to greater achievement, who so patiently supported me throughout the hard times of my work. Thanks to my children, Hurul Ain and Muhammad Mustaqiim for their faith and pride in their mom. Last but not least, I want to thank my mother for her love and dedications for raising me, supporting me and educating me.



ABSTRACT

Two-fluid mixing is an essential process in many microfluidic devices for Biomedical Micro-Electro-Mechanical Systems (BioMEMS) applications. For example, various biomedical and biochemical process involve the mixing of two fluids. The performance of such processes relies on effective and rapid mixing of samples and reagents. This project discussed the mixing characteristics of two fluids with different properties in term of Reynolds number (Re) with Y-Shape glass based micromixer. Blood flow properties was used to be mixed with a particular type of reagents which the difference in the properties of these two mixing fluids will be adjusted by varying the viscosity. The laminar mixing of the two fluids inside these micromixers was simulated at low (<<1) Re flow. The Reynolds number parameters consist of v_s , mean fluid velocity in m s⁻¹, L is the characteristic length in m, μ is the absolute dynamic fluid viscosity in kgm⁻¹s⁻¹, and ρ is the density of the fluid in kgm⁻³. Simulation and visualizations results were obtained using CoventorWare2006. The mixing characterization will be based on the visualization results of the distribution field in term of viscosity. In this study it was found that higher Reynolds number will results in better mixing and smaller mixing channel width.



ABSTRAK

Percampuran dua jenis bendalir adalah satu proses penting dalam kebanyakan peranti bendalir mikro bagi aplikasi BioMEMS. Sebagai contoh, pelbagai proses bioperubatan dan bio-kimia melibatkan percampuran antara dua bendalir. Prestasi bagi proses tersebut bergantung kepada kepantasan percampuran antara sample dan reagen. Projek ini akan membincangkan tentang ciri-ciri percampuran dua bendalir yang mempunyai perbezaan sifat; dari segi nombor Reynolds pada pencampur mikro berbentuk-Y berasaskan kaca. Sifat pengaliran darah digunakan untuk dicampur dengan beberapa jenis reagen dimana perbezaan sifat kedua-dua bendalir ini diubah dengan mengubah nilai kelikatannya. Percampuran laminar antara dua bendalir didalam pencampur mikro ini disimulasi pada pengaliran nombor Reynolds rendah (<<1). Parameter bagi nombor Reynolds terdiri daripada v_s , iaitu kelajuan bendalir dalam unit in m s⁻¹, L ialah panjang dalam unit m, μ ialah kelikatan dinamik bendalir dalam unit kgm⁻¹s⁻¹, dan ρ ialah ketumpatan bendalir dalam unit kgm⁻³. Simulasi dan keputusan visual didapati menggunakan perisian CoventorWare2006. Ciri-ciri percampuran dibuat berdasarkan keputusan visual bagi kelikatan bendalir. Dalam kajian ini didapati nombor Reynolds yang tinggi akan memberi kesan percampuran yang lebih baik dan lebar mixing channel yang lebih kecil.



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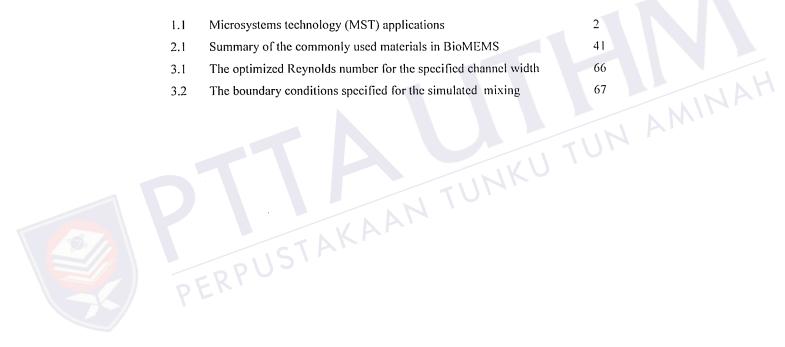
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LIST OF SYMBOL

a	-	acceleration
d	-	diameter
dS	-	elemental surface area
F	-	force vector
$ar{g}$	-	gravitational acceleration
L	-	characteristic length
m	-	mass of the body
μ	-	dynamic viscosity
ñ	-	characteristic length mass of the body dynamic viscosity unit vector normal to the surface
p	-	pressure
ρ	-	pressure mass density volume flow rate
Q	-	volume flow rate
R	-	position vector
Re	-19	Reynolds number
SER		control surface
t	-	time
τ	-	shear stress
u _o	-	velocity
u(y)	-	velocity of the fluid at a distance y
V	-	fluid's velocity
υ	-	control volume
ν	-	kinematic viscosity
\overline{v}	-	flow velocity

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LIST OF ABBREVIATIONS

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Ab	-	Antibody
Ag	-	Antigen
BEM	-	Boundary Element Method
BioMEMS	-	Biomedical Micro Electro Mechanical Systems
CAD	-	Computer Aided Design
CE	-	Capillary Electrophoresis
CFD	-	Capillary Electrophoresis Computational Fluid Dynamics
DNA	-	Deoxyribonucleic acid
DRIE	-	Deep reactive-ion etching
ELISA	-	Enzyme-linked immunosorbent assay
FDM	-	Finite Difference Method
FEM	<u>v</u>	Finite Element Method
FVM	-	Finite Volume Method
HPLC	-	High Performance Liquid Chromatography
IA	-	Immunoassays
LIGA	-	Lithographie Galvanoformung Abformung
LOC	-	Lab-on-a-chip
MAFIAS	-	Micro Ammonia Flow Injection Analysis System

MEMS Micro-Electro-Mechanical Systems -MST Microsystem Technology μTAS Micro-Total-Analysis Systems -ODE Ordinary Differential Equations -Polymerase Chain Reaction PCR _ Ribonucleic acid RNA -WBC White blood cells -

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PUBLICATIONS

- Intan Sue Liana Abdul Hamid, Ahmad Alabqari Ma'Radzi and Muhammad Mahadi Abdul Jamil (2008). "Low Reynolds Number Effect In Designing Y-Shape Micromixer For BioMEMS Application." 2nd International Conference on Science & Technology: Applications in Industry & Education 2008 (ICSTIE'08), Penang, Malaysia.
- 2. Intan Sue Liana Abdul Hamid, Ahmad Alabqari Ma'Radzi and Muhammad Mahadi Abdul Jamil (2008). "Viscosity Effect on Low Reynolds Number Mixing In Y-Micromixer." 6th Student Conference on Research and Development 2008 (SCOReD2008), UTM Skudai, Malaysia.



CHAPTER I

INTRODUCTION

1.1 Background



Micro-electro-mechanical systems (MEMS) technologies have been developed over the past 20 years for a diverse range of applications from automotive to medical devices. The development of miniature analytical devices with sophisticated functionality in the field of medical and life sciences is the result of recent advances of microsystem technology (MST) to biomedical applications (BioMEMS). Microsystems (so called lab-on-a-chip, biochips, microchips), which are based on integrating large parallel arrays of miniaturized fluidic components and sensors into the smallest possible space, provide a lot of advantages. In recent years, the demand for high-precision miniature devices and efficient processing technologies for micro-/nano-fabrication has been growing rapidly. The various fields of MST applications are listed in Table 1.1.

Application field	Devices		
Chemical and medical	Gene-chips, hearing aids, drug delivery systems, bio-sensors, fuel cells.		
Telecommunication and optical	Diffraction gratings, miniature lens and		
components	mirrors.		
Automotive	crash, acceleration and distance sensors		
Mechanical	Printer heads, micro heat exchangers,		
Meenamear	camera and watch components.		

 Table 1.1
 Microsystems technology (MST) applications.

1.1.1 BioMEMS



BioMEMS, or biomedical micro-electro-mechanical systems, has emerged as a subset of MEMS devices for applications in biomedical research and medical microdevices. The classes of BioMEMS devices commonly found including microsensing, microactuation, microassaying, micromoving and microdelivery. BioMEMS is a science that includes more than simply finding biomedical applications for MEMS devices. It represents an expansion into a host of new polymer materials, microfluidic physics, surface chemistries and modification, 'soft' fabrication techniques including polymers and biological components, biocompatibility, and cost-effective solutions to biomedical problems. BioMEMS devices are unique because they bring together the creative talents of electrical, mechanical, optical, and chemical engineers, materials specialists, clinical laboratory scientist, and physicians. Miniaturization is important in biomedical applications since we will include sample size from submicron to micron range, for instance the genes, protein and deoxyribonucleic acid (DNA).

BioMEMS devices can typically be considered as having at least one feature's dimension in the submicron to micron range (~100nm-200 μ m), and other dimensions of up to several millimeters. On one end of the application scale they may be the platform for nanotechnologies, while on the other end they may be the key component to a much larger device such as a medical imaging machine. They may be all encompassing devices, but more typically they are integrated with other component and perform one or more functions in a chain of operations connected by tubing or other conduits. Among the advantages of biochip miniaturization are lower manufacturing costs, reproducibility, small sample size, and reagent use. Improved signal-to-noise ratio, improved response time, precise control of mixing, reacting, and discarding of waste products, in-line or embedded detection methods, and high throughput are also advantages of miniaturization biochips (Steven, 2006). The acceleration of new biomedical instrumentation in recent years is due in part to demand for higher-quality medical care, especially in highly developed countries (Dario et al., 2000). By improving current techniques for sample preparation and assay of blood, urine, cerebral spinal fluid, extracts, cells, cultures, and tissues; diagnostic systems can be improved.



1.1.2 Micro-Total Analysis Systems (M-TAS) and Lab-On-A-Chip (LOC)

Micro-total-analysis systems (µTAS), and the subset of devices referred to as lab-on-a-chip (LOC), derive from application of "hard" and "soft" fabrication techniques for the manufacture of miniaturized devices that perform all or part of a biochemical analysis. µTAS may be hybrids of multiple chips, integrated electronics, and external supports; while LOC refers more specifically to a microfluidic chip or other device that performs a well-defined analytical task. Lab-on-a-chip (LOC) is a term for devices that integrate (multiple) laboratory functions on a single chip of only millimeters to a few square centimeters in size and that are capable of handling extremely small fluid volumes down to less than pico liters. The small size and portability of lab-on-a-chip systems are very advantageous. LOC greatly reduce reagent volume, sample contamination, and power consumption. It can also provide faster and more efficient compounding and separations in biomedical and analytical applications. The miniaturization also results in a significant improvement of lab safety. For example, spills, explosions, and other laboratory accidents that can occur during conventional sample preparation procedures are not a problem with the lab-on-a-chip devices due to the extremely small amount of sample used.

1.1.3 Microfluidics



Design and implementation of necessary microfluidic functions; integration of these functions with complete automation; and development of cost-effective manufacturing technology are the major technical challenges in making these microsystems. Microfluidics covers the science of fluidic behaviors on the micro/nanoscales and the design engineering, simulation, and fabrication of fluidic devices for transport, delivery, and handling of fluids on the order of microliters or smaller volumes. It is the backbone of biological or biomedical microelectromechanical systems (BioMEMS) and lab-on-chip concept, as most of biological analyses involve fluid transport and reaction.

Biological or chemical reactions on the micro/nanoscale are usually rapid since small amounts of samples and reagents are used, which offers quick and low-cost analysis. Major microfluidic components include sample introduction or loading (and in some cases, sample preparation); propulsion of fluids (such as samples to be analyzed, reagents, and wash and calibration fluids) through micron-sized channels;

valving; fluid mixing and isolation as desired; small volume sample metering; sample splitting and washing; and temperature control of the fluids. The main challenge in making miniaturized systems is the integration of different microfluidic components to perform certain functions at high speed and high throughput.

1.1.4 MEMS CAD Tools for Microfluidic Application

Due to the nature of MEMS devices, especially its size and manufacturing cost, it would be very difficult if not impossible to create without first designing and visualizing them. With a simulation tool, it is easier, faster and much less expensive to build a MEMS device. It is absolutely necessary to use a simulation tool so that the time it takes from designing to completion of the component is reduced significantly. It is less cost to modify, if there are mistakes in the design, before it is actually prototyped or manufactured. A simulation tool can be used to predict and improve device characteristics. The accurate analysis of these characteristics leads to an optimization of the device and hence improves system performance.



A typical computer aided design (CAD) should have three basic components; a geometry builder where the geometry of the device could be drawn, a simulation module where the problem is solved using the relevant governing equations, and a visualization module where the simulation results can be displayed (Korsmeyer *et al.*, 2004). In order to create useful MEMS fluidic devices, the CAD tool must have as its underlying principle the models that definitively characterize the operation of the device. Such CADs must be able to handle fluids within the length scales that involve both noncontinuum fluid effects molecular models as well as continuum models (White, 2004).

CAD tools can be categorized as either field-solvers or network simulators. Field-solvers can solve complex partial differential equations, using finite element method (FEM) or boundary-element method (BEM). These equations are a detailed description of the physical design of the MEMS device. They are complex equations taking a lot of time to solve. Network simulators are required for system level modeling. These give a description of the system with a building-block orientation. Simpler ordinary differential equations are used to describe the system. For the design of MEMS, field-solvers are available and are widely used, such as ANSYS / *Multiphysics*. System-level tools are also available, such as *CoventorWare* and *Saber*. This project will be using the CoventorWare2006 software; where once the behavior of the entire device is understood and promising design identified, detailed numerical AN TUNKU TUN AMINA modeling can then be carried out in order to confirm the system-level results and to optimize the design parameters.

1.2 **Objective of Study**

Objectives for this research are:

- a) To find an optimum design of micromixer in term of Reynolds number by analysis and characterization of various lengths and width of Y-shape micromixer design.
- b) To design and simulate micromixer for laminar fluid mixing of two fluids with various viscosity using CoventorWare2006 software.
- c) To characterize the diffusion properties in micromixer.

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