

MIXED CONVECTION IN A LID-DRIVEN
ENCLOSURE FILLED WITH HYBRID
NANOFLUID BY FINITE VOLUME METHOD

INAS RIDHA ALI

A thesis submitted in
fulfillment of the requirement for the award of the
Degree of Doctor of Philosophy in Science

Faculty of Applied Sciences and Technology
Universiti Tun Hussein Onn Malaysia

MAY 2022

DEDICATION

To my inspiration and my support (God). To the pulse of my soul and my heart, my (mother). To the master of my life and my beloved (Ali). To a flower of the heart and my eternal love for my (son).



ACKNOWLEDGEMENT

First and foremost, praise and thanksgiving to Allah for the blessing of mind and health and unwavering support to complete this thesis. In addition, I would like to express my utmost gratitude and appreciation to my main supervisor Dr. Norhaliza Binti Abu Bakar, co-supervisor Prof. Dr. Rozaini Roslan for their encouragement, advices, guidance, constructive suggestions to me for developing a full understanding of this research journey. And a very special thanks and gratitude to Assoc. Prof. Dr. Ammar Ibraheem Alsabery for his constructive scientific advice, constant encouragement and guidance that give me confidence. The special feeling of gratitude to my husband and my love and my soul (Ali) whose words of encouragement and push for tenacity ring in my ears. Moreover, special thanks to my lovely mom for her continuous support throughout my life as well as to my son (Yahia).



PTTA UTHAM
PERPUSTAKAAN TUNKU TUN AMINAH

ABSTRACT

The heat transfer process in complex geometries is essential due to its wide range of industrial and engineering applications. Understanding fluid flow patterns and convection heat transfer will give scientists or engineers the idea to manipulate the process to achieve the desired results. For the past decade, researchers reported that nanofluid enhances heat transfer and fluid flow. With rapid development in engineering, scientists and engineers have begun to study the fluid flow and heat transfer pattern of hybrid nanofluids. However, there are still many gaps to be filled in. This study will simulate the steady mixed convection flow in a single or double lid-driven cavity filled with hybrid nanofluid ($\text{Al}_2\text{O}_3\text{-Cu-water}$). The fluid is assumed to be Newtonian and laminar. The flow is two-dimensional and incompressible. Nanoparticles are assumed in a spherical shape. Firstly, the fluid flow pattern and heat transfer behavior on mixed convection in a lid-driven square cavity filled with hybrid nanofluid with cold sidewalls was studied. The bottom wall was uniformly heated, while the top wall was adiabatic. Mixed convection in a double lid-driven horizontal rectangular cavity filled with hybrid nanofluid was determined in the second problem. Non-uniform heating distribution on both horizontal walls was studied in the third problem. Finally, the inclined magnetic field's influences and cavity on mixed convection in a lid-driven rectangular cavity-filled hybrid nanofluid were analyzed. The dimensionless governing equations were formulated by using appropriate reference variables. These equations were solved using the finite volume method. The convection-diffusion terms were discretized using the power-law scheme, while the pressure and velocity components were coupled using the SIMPLE algorithms. The resultant matrices were then solved iteratively using the Tri-Diagonal Matrix Algorithm coded in FORTRAN90. The present solutions obtained were then compared with previous studies, and a good agreement was found. The numerical results were presented in the forms of isotherm and streamline. The results show that the flow circulation strength is enhanced by the hybrid nanofluid addition due to the hybrid nanoparticles' higher thermal conductivity compared with the nanofluids.

ABSTRAK

Proses pemindahan haba dalam geometri kompleks adalah sangat penting kerana penggunaannya oleh aplikasi dalam bidang kejuruteraan dan industri yang meluas. Memahami corak aliran bendalir dan pemindahan haba perolakan akan memberi idea kepada saintis atau jurutera untuk memanipulasi proses tersebut bagi mencapai hasil yang diinginkan. Selama berdekad yang lalu, para penyelidik melaporkan bahawa bendalir nano meningkatkan pemindahan haba dan aliran cecair. Dengan perkembangan pesat dalam bidang kejuruteraan, saintis dan jurutera telah mula mempelajari aliran bendalir dan corak pemindahan haba bendalir nano kacukan. Walau bagaimanapun, masih ada banyak jurang yang harus diisi. Kajian ini akan mensimulasikan aliran perolakan campuran mantap dalam rongga dengan satu atau dua penutup yang bergerak yang dipenuhi dengan bendalir nano kacukan ($\text{Al}_2\text{O}_3\text{-Cu}$ -air). Bendalir tersebut dianggap sebagai Newtonian dan lamina. Alirannya adalah dua dimensi dan tak termampatkan. Partikel nano diandaikan berbentuk sfera. Pertamanya, corak aliran bendalir dan tingkah laku pemindahan haba pada perolakan campuran dalam rongga bersegi empat yang dipenuhi bendalir nano kacukan dengan dinding sisi yang sejuk telah dikaji. Dinding bawah dipanaskan secara seragam sementara dinding atas tertebat. Perolakan campuran dalam rongga segi empat tepat mendatar dengan penutup bergerak berganda dipenuhi dengan bendalir nano kacukan telah dikaji pada masalah kedua. Pemanasan secara tidak seragam pada kedua-dua dinding melintang telah dikaji pada masalah ketiga. Akhir sekali, kesan medan magnet dan rongga yang condong pada aliran perolakan campuran dalam rongga segi empat tepat dengan satu dinding bergerak dipenuhi bendalir nano kacukan dianalisis. Persamaan menakluk tak bermatra telah dirumuskan dengan menggunakan pemboleh ubah rujukan yang sesuai. Persamaan tersebut diselesaikan menggunakan kaedah isipadu terhingga. Sebutan perolakan-resapan didiskritkan menggunakan skema hukum kuasa sementara komponen tekanan dan halaju digabungkan menggunakan algoritma SIMPLE. Matriks yang dihasilkan telah diselesaikan secara tertelar dengan menggunakan Algoritma Matrik Tiga Penjuru dan dikodkan dalam FORTRAN90. Penyelesaian yang diperoleh telah dibandingkan dengan kajian yang terdahulu dan mendapat keputusan yang baik.

Keputusan berangka dibentangkan dalam bentuk isoterma dan garis arus. Hasil kajian menunjukkan bahawa kekuatan peredaran aliran ditingkatkan dengan penambahan bendalir nano kacukan kerana kekonduksian terma bendalir nano kacukan yang lebih tinggi berbanding dengan bendalir nano.



CONTENTS

	TITLE	i
	DECLARATION	ii
	DEDICATION	iii
	ACKNOWLEDGEMENT	iv
	ABSTRACT	v
	ABSTRAK	vi
	CONTENTS	viii
	LIST OF TABLES	xiii
	LIST OF FIGURES	xiv
	LIST OF SYMBOLS	xix
	LIST OF PUBLICATIONS	xxii
CHAPTER 1	INTRODUCTION	1
	1.1 General introduction	1
	1.2 Fluid mechanics	2
	1.3 Hybrid nanofluids	4
	1.4 Heat transfer	6
	1.4.1 Thermal conduction	6
	1.4.2 Thermal convection	7
	1.4.3 Thermal radiation	9
	1.5 Magnetohydrodynamics	10
	1.6 Numerical solutions in fluids dynamics	11
	1.7 Dimensionless numbers in fluids dynamics	12
	1.8 Problem statement	13
	1.9 Objectives	13
	1.10 Scope of research	14
	1.11 Significant of study	15
	1.12 Thesis organization	16
CHAPTER 2	LITERATURE REVIEW	18

2.1	Introduction	18
2.2	Mixed convection in cavities:	18
2.2.1	Square cavity	19
2.2.2	Rectangle cavity	28
2.3	Heat transfer applications of hybrid nanofluids	29
2.4	Magnetic field	31
2.5	Sinusoidal heating	33
2.6	Double lid - driven cavity	35
2.7	Lid - driven cavity lower wall is heated and the vertical walls cooling	36
2.8	Conclusions	37
CHAPTER 3	RESEARCH METHODOLOGY	39
3.1	Introduction	39
3.2	Boussinesq approximation	39
3.3	Derivation of conservation equations	41
3.3.1	Conservation of mass	42
3.3.2	Conservation of momentum	44
3.3.3	Conservation of energy	47
3.4	Problems nature	48
3.5	Finite volume method	49
3.5.1	General differential equation	50
3.5.2	Discretization equation	50
3.5.3	Calculation of flow field	58
3.5.4	Solution of discretized equations	66
3.6	Problem formulation	67
3.6.1	Dimensionless parameters	68
3.6.2	Mixed convection in a lid-driven square cavity filled hybrid nanofluid with cold sidewalls and heated bottom wall using finite volume method	68

3.6.3	Mixed convection in a double lid-driven horizontal rectangular cavity filled with hybrid nanofluid by using finite volume method	72
3.6.4	Mixed convection in a double lid-driven rectangular cavity filled by a hybrid nanofluid with non-uniform heating distribution on both horizontal walls using finite volume method	74
3.6.5	Influences of inclined magnetic field and inclined cavity on mixed convection in a lid-driven rectangular cavity filled hybrid nanofluid ($\text{Al}_2\text{O}_3\text{-Cu-water}$) using finite volume method	75
3.6.6	Numerical method	78
CHAPTER 4	MIXED CONVECTION IN A LID-DRIVEN SQUARE CAVITY FILLED HYBRID NANOFLUID WITH COLD SIDEWALLS AND HEATED BOTTOM WALL	81
4.1	Introduction	81
4.2	Mathematical formulation	82
4.3	Dimensionless process	82
4.4	Numerical method	88
4.5	Results and discussion	90
4.6	Conclusions	100
4.7	Contribution	100
CHAPTER 5	MIXED CONVECTION IN A DOUBLE LID-DRIVEN HORIZONTAL RECTANGULAR CAVITY FILLED WITH HYBRID NANOFLUID	102

5.1	Introduction	102
5.2	Mathematical formulation	103
5.3	Dimensionless process	103
5.4	Numerical method	104
5.5	Grid-independence test	104
5.6	Results and discussion	105
5.7	Conclusions	115
5.8	Contribution	115
CHAPTER 6	MIXED CONVECTION IN A DOUBLE LID-DRIVEN RECTANGULAR CAVITY FILLED BY A HYBRID NANOFLUID WITH NON-UNIFORM HEATING DISTRIBUTION ON BOTH HORIZONTAL WALLS	117
6.1	Introduction	117
6.2	Mathematical formulation	118
6.3	Dimensionless process	118
6.4	Numerical method	119
6.5	Grid-independence test	119
6.6	Results and discussion	121
6.7	Conclusions	131
6.8	Contribution	132
CHAPTER 7	INFLUENCES OF INCLINED MAGNETIC FIELD AND INCLINED CAVITY ON MIXED CONVECTION IN A LID-DRIVEN RECTANGULAR CAVITY FILLED HYBRID NANOFLUID (Al₂O₃-Cu-WATER)	133
7.1	Introduction	133
7.2	Mathematical formulation	134
7.3	Dimensionless process	134
7.4	Numerical method	135
7.5	Grid-independence test	135
7.6	Results and discussion	137

7.7	Conclusions	152
7.8	Contribution	152
CHAPTER 8	CONCLUSIONS AND RECOMMENDATIONS	154
8.1	Introduction	154
8.2	Summary of research	154
8.3	Recommendations for future research	156
	REFERENCES	157
	APPENDIX	178
	VITA	195



PTTA UTHM
PERPUSTAKAAN TUNKU TUN AMINAH

LIST OF TABLES

3.1	Function $A(\varphi)$ for different scheme	58
4.1	Thermo-physical properties of water, Cu, Al_2O_3 nanoparticles at $T = 310\text{K}$	91



PTTA UTHM
PERPUSTAKAAN TUNKU TUN AMINAH

LIST OF FIGURES

1.1	Fluid mechanics overview	4
1.2	The difference between a nanofluid and a hybrid nanofluid	6
1.3	The three methods of heat transfer	10
1.4	Objectives outlines	14
1.5	Thesis outlines	17
3.1	Elemental control volume in a flow field for the derivation of the continuity equation	44
3.2	The finite size control volume	46
3.3	A part of the two dimensional grid	51
3.4	Control volume for the two dimensional situation	52
3.5	Variation of A and B with Peclet number	55
3.6	A u -control volume and its neighboring velocity components	60
3.7	A v -control volume and its neighboring velocity components	61
3.8	Control volume for the continuity equation	63
3.9	Numerical solution flow chart of SIMPLE algorithm	65
3.10	Schematic of the problem of mixed convection in a lid-driven square cavity filled by a hybrid nanofluid with left and right cold walls, insulated movable upper wall, and a hot fixed bottom wall	71
3.11	Schematic of the problem of mixed convection in a double lid-driven horizontal rectangular cavity filled with hybrid nanofluid by using finite volume method	73
3.12	Schematic of the problem of mixed convection in a double lid-driven rectangular cavity filled by a hybrid nanofluid with non-uniform heating distribution on both horizontal walls using finite volume method	75
3.13	Schematic of the problem of influences of inclined magnetic field and inclined cavity on mixed convection in a lid-driven rectangular cavity filled hybrid nanofluid (Al_2O_3 -Cu-water) using finite volume method	77

3.14	Schematic of inclined magnetic field imposed to the cavity	77
3.15	Uniform grid	79
3.16	Illustration chart of the third chapter	80
4.1	Average Nusselt number variation along the hot wall with grid sizes	88
4.2	Comparison of isotherms between experimental outcomes	89
4.3	Comparison numerical results	90
4.4	Stream function and temperature contours for uniformly heated bottom wall and cooled right and left walls with $\varphi = 0, 0.01, 0.03, 0.04$	94
4.5	Stream function and temperature contours for uniformly heated bottom wall and cooled right and left walls with $Re = 5, 50, 250, 500$	95
4.6	Stream function and temperature contours for uniformly heated bottom wall and cooled right and left walls with $Ri = 0.01, 0.1, 1, 10$	96
4.7	The evolution of the average Nusselt number as a function of various volume fractions of nanoparticles φ for the base fluid, nanofluids and hybrid nanofluids	97
4.8	The evolution of the average Nusselt number as a function of various volume fractions of nanoparticles Re for the base fluid, nanofluids and hybrid nanofluids	97
4.9	Variation of average Nusselt number with Re for different φ	98
4.10	Variation of local Nusselt number interfaces with X for different Re with $\varphi = 0.02$ and $Ri = 1$	98
4.11	Variation of local Nusselt number interfaces with X for different Ri with $\varphi = 0.02$ and $Re = 100$	99
4.12	Variation of velocity profile along the vertical direction at x -axis with different Ri	99
4.13	The flowchart of the used numerical code	101
5.1	Average Nusselt number variation along the hot wall with grid sizes	104

5.2	Comparison of present study	105
5.3	Stream function and temperature contours for heated bottom wall and cooled up wall with length $\varphi = 0.0, 0.04$	108
5.4	Stream function and temperature contours for heated bottom wall and cooled up wall with length $Ri = 0.01, 0.1, 1, 10$	109
5.5	Stream function and temperature contours for heated bottom wall and cooled up wall with length $Re = 10, 50, 250, 500$	110
5.6	Stream function and temperature contours for heated bottom wall and cooled up wall with effect of direction of the moving walls	111
5.7	Stream function and temperature contours for heated bottom wall and cooled up wall with length $L = 0.5, 1, 1.5, 2.5$	112
5.8	Variations of the average Nusselt-number with Re for different L	113
5.9	Variations of the velocity U with Re for different L	113
5.10	Variations of the average Nusselt-number with Re for different φ	114
5.11	Variations of the velocity U with Re for different φ	114
6.1	Average Nusselt number variation along the top and bottom walls with grid sizes	120
6.2	Comparison of present study with Sarris et al. (2010) for $Ra_f = 10^5$, $\varphi = 0$ and $Pr_f = 100$	120
6.3	Stream function and temperature contours for non-uniformly heated up and down walls with $Re = 2, 10, 50, 100, 200$	125
6.4	Stream function and temperature contours for non-uniformly heated up and down walls with effect of direction of the moving walls	126
6.5	Stream function and temperature contours for non-uniformly heated up and down walls with effect of phase deviation $\Omega = 0, \frac{\pi}{4}, \frac{3\pi}{4}, \pi$	127

6.6	Stream function and temperature contours for non-uniformly heated up and down walls with effect of amplitude ratio $\varepsilon = 0, 0.3, 0.7, 1$	128
6.7	(a) Variation of average Nusselt number interfaces with Re for different phase deviation Ω . (b) Variation of average Nusselt number interfaces with Re for different amplitude ratio ε	129
6.8	(a) Variation of average Nusselt number interfaces with Re for different φ . (b) Variation of the of average Nusselt number with φ for different types particles	129
6.9	Variation of local Nusselt number interfaces with Y for different amplitude ratio ε for Al_2O_3 -Cu-water	130
6.10	Variation of local Nusselt number interfaces with Y for different phase deviation γ for Al_2O_3 -Cu-water	130
6.11	Variation of local Nusselt number interfaces with Y for different Re for Al_2O_3 -Cu-water	131
7.1	Average Nusselt number variation along the hot wall with grid sizes	136
7.2	Comparison of present results with Soong and Tzeng (1996) and Ghasemi and Aminossadati (2009)	136
7.3	Stream function and temperature contours for heated bottom wall and cooled up wall with effect of Re	142
7.4	Variation of the steady local Nusselt number interfaces with X for different Re	143
7.5	Variation of velocity profile along the vertical direction at x -axis with different Re	143
7.6	Stream function and temperature contours for heated bottom wall and cooled up wall with effect of Hartmann number	144
7.7	Variation of the steady local Nusselt number interfaces with X for different Ha	145
7.8	Variation of velocity profile along the vertical direction at x -axis with different Ha	145

7.9	Stream function and temperature contours for heated bottom wall and cooled up wall with effect of magnetic field inclination	146
7.10	Variation of the steady local Nusselt number interfaces with X for different γ	147
7.11	Variation of velocity profile along the vertical direction at x -axis with different γ	147
7.12	Stream function and temperature contours for heated bottom wall and cooled up wall effect of cavity inclination	148
7.13	Variation of the steady local Nusselt number interfaces with X for different ω	149
7.14	Variation of velocity profile along the vertical direction at x -axis with different ω	149
7.15	Average Nusselt number with (a) φ and (b) γ for various types of nanoparticles at $\varphi = 0.02$, $L = 3$, $Ri = 1$, $Re = 100$, $\gamma = \frac{\pi}{4}$, $Ha = 20$, $\omega = 45^\circ$ and $Pr = 6.2$	150
7.16	Average Nusselt number with (a) Re and (b) ω for different values of φ at hybrid nanofluid at $L = 3$, $Ri = 1$, $\gamma = \frac{\pi}{4}$, $Ha = 20$ and $Pr = 6.2$	150
7.17	Average Nusselt number with (a) γ for different values of φ at hybrid nanofluid and (b) γ for different values of Ha at hybrid nanofluid at $L = 3$, $Ri = 1$, $\omega = 45^\circ$ and $Pr = 6.2$	151
7.18	Average Nusselt number with (a) Re for different values of γ at hybrid nanofluid and (b) γ for different values of ω at hybrid nanofluid at $L = 3$, $Ri = 1$, $Ha = 20$ and $Pr = 6.2$	151

LIST OF SYMBOLS

a	- power law expressions
A	- dimensionless coefficient of Peclet number
b	- simplified variable
CV	- control volume
D	- diffusion conductance
E	- electric field
f	- element of body force
F	- body force
F	- general force
g	- gravitational acceleration, m/s^2
Gr	- Grashof number
h	- heat transfer coefficient
J	- total fluxes
J_E	- current density
L	- length of the rectangular cavity, m
m	- number of grid point in x - direction
M	- mass flow
n	- number of grid point in y - direction
\overline{Nu}	- average Nusselt number
Nu_x	- local Nusselt number
p	- pressure, Pa
\mathcal{P}	- dimensionless pressure

- ρ - Peclet number
 Pr - Prandtl number
 Re - Reynolds number
 Ri - Richardson number
 T - temperature, $^{\circ}C$
 u, v - velocities in the x – and y – direction respectively
 U, V - dimensionless velocity in X – and Y – direction respectively
 U_0 - lid velocity, m/s
 V - velocity vector
 x, y - Cartesian coordinates
 X, Y - dimensionless Cartesian coordinates
 d_f - molecular diameter of water
 l_f - path of fluid particles
 k_b - Boltzmann constant $k_b = 1.380648 \times 10^{-23} (J/K)$
 Re_B - Brownian motion Reynolds number
 T_0 - reference temperature (310K)
 u_B - Brownian velocity of the nanoparticle

Greek Letter

- α - thermal diffusivity
 β - thermal expansion coefficient
 γ - magnetic field inclination angle
 ε - amplitude ratio
 θ - dimensionless temperature
 μ - dynamic viscosity
 ν - kinematic viscosity

ρ	- density
ν_f	- kinematic viscosity of the fluid (m^2/s)
Ω	- phase deviation
ϕ	- general variable
Φ	- dissipation
φ	- solid volume fraction
ω	- cavity inclination

Subscripts

b	- bottom
c	- cold
f	- fluid
h	- hot
l	- left
r	- right
nf	- nanofluid
hnf	- hybrid nanofluid
t	- top
∞	- reference state

Superscripts

\circ	- old value
$*$	- guess value
$'$	- correction value

LIST OF PUBLICATIONS

1. I.R. Ali, Ammar I. Alsabery, N.A. Bakar and Rozaini Roslan “Mixed Convection in a Double Lid-Driven Cavity Filled with Hybrid Nanofluid by Using Finite Volume Method” *Symmetry* 12, no. 12 (2020). <https://doi.org/10.3390/sym12121977>. (ISI) (Impact factor 2.645)
2. I.R. Ali, Ammar I. Alsabery, N.A. Bakar and Rozaini Roslan “Mixed Convection in a Lid-Driven Horizontal Rectangular Cavity Filled with Hybrid Nanofluid By Finite Volume Method”. *Journal of Advanced Research in Micro and Nano Engineering*.



PTTA UTHM
PERPUSTAKAAN TUNKU TUN AMINAH

CHAPTER 1

INTRODUCTION

1.1 General introduction

Considering the expansive scope of uses, such as greasing system polymer processing, chemical processing apparatus, hydrodynamic machinery, building ventilation, electronic hardware, the investigation of natural convection, forced and combined convection heat transfer and fluid momentum has been regarded as one of the most important research topics. Moreover, during recent years, many studies have focused on heat transfer mixed convection in cavities due to its widish applications in industry, such as electronic refrigeration devices, food storage, and lubrication technologies Morzynski and Popiel (1988). Despite its wide applications, its convection heat transfer performance has been characterized by its poor adequacy due to the low thermal conductivity of the convection fluid. To improve the heat transfer properties of the liquid, numerous numerical and experimental investigations have been performed utilizing different methods such as the use of extended surfaces including fins, microfins, vortex flow devices, jet impingement, electromagnetic field, ultra-high thermal conductivity composite materials, and phase-change devices. Moreover, there are different methods to improve the effectiveness of heat transfer.

In general, there are two groups of technologies for intensifying heat transfer. The first set of technologies is required for external energy input by mechanical

vibration, rotation, mixing, and addition of external magnetic or electrostatic field, which has been utilized effectively to improve heat and mass transfer. However, external power inputs are expensive and difficult under compacted situations. In the second group of techniques, the heat transfer magnification can be attained by modifying fluids property by adding nanoparticles, surface shape changes, surface area enhancement, and disorder. Geometric shapes play an adequate role in controlling the velocity of flow and heat distribution in the region. From a convection standpoint, flows over rotating or stationary surfaces are important for the thermal design of different types of industrial equipment, such as nuclear waste disposal cans, rotating heat exchangers, nuclear reactor cooling systems, rotating stable rockets, and geothermal tanks. In the ongoing past decades, many researchers have been interested in obtaining solutions to the problems of the thermal transfer phenomenon that occur in fluid dynamics, plasma physics, aerodynamics, and meteorology utilizing various procedures. One of these is the numerical techniques used to predict flow behaviors and heat transfer performance. In this study, the mixed convection with hybrid nanofluids ($\text{Al}_2\text{O}_3\text{-Cu-water}$) in a lid-driven cavity was studied. The bottom wall was maintained at temperatures T_h and vertical walls were maintained at temperatures T_c and adiabatic. The effects of the magnetic field, inclination angle, and sinusoidal heating method on the flow field were investigated.

In the next sections, the topic of heat transfer with hybrid nanofluids is introduced, focusing on mixed convection. In the current study, the dimensionless non-linear partial differential equations subjected to the given boundary conditions were solved numerically.

1.2 Fluid mechanics

The liquid state in physics and chemistry is one of the three states related to thermodynamics, along with the gaseous state and the solid-state. A liquid is a fluid that has a constant volume at temperature and pressure, which takes the shape of the container it contains. The liquid also applies pressure to the surface of the container in the same way that the liquid applies pressure to anything inside. Liquids tend to have better thermal conductivity than gases, and the ability to flow makes a liquid suitable for removing excess heat from mechanical components Vargaftik (1993). Also, the

fluid is known as a substance that continuously deforms (flows) under the action of shear stress. Liquids can be divided into two stages, liquids, and gases. The gas is constantly expanding and occupying the full volume of any container Cohen (2010). The density of a gas is much less than that of a liquid. As a result, force and pressure are found in fluid mechanics where the weight of any type of fluid plays an important role compared to the weight of a gas Massey (2006).

Fluid mechanics is the branch of physics that deals with the mechanics of fluids (liquids, gases, and plasmas) and the forces they exert on them. It has applications in a wide range of disciplines, including mechanical, civil, chemical, and biomedical. Engineering, geophysics, oceanography, meteorology, astrophysics, biology, including those containing computing forces and moments on aircraft, limiting the volume flow measurement of petroleum through pipelines, forecasting weather models, comprehending nebulae in interstellar space, and modeling fission weapon detonation. Some of its laws are even employed in traffic engineering, where traffic is considered as a continuous fluid.

It can be divided into fluid statics, the study of fluids at rest, and fluid dynamics, the study of the effect of forces on the movement of fluids. Streeter and Wylie (1979) It is a branch of continuum mechanics, a subject that models matter without using the information that it is made of atoms; that is, it models matter from a macroscopic rather than a microscopic point of view. Fluid mechanics, especially fluid dynamics, is an active field of research, typically mathematically complex. Many problems are totally or partially unsolved and are best approached by numerical methods, usually using computers. A modern discipline, called computational fluid dynamics (CFD), is dedicated to this approach nature of the fluid flow. As shown in Figure 1.1.

REFERENCES

- Abbasian Arani, A. A., S. Mazrouei Sebdani, M. Mahmoodi, A. Ardeshiri, and M. Aliakbari. 2012. "Numerical Study of Mixed Convection Flow in a Lid-Driven Cavity with Sinusoidal Heating on Sidewalls Using Nanofluid." *Superlattices and Microstructures* 51 (6): 893–911.
- Abu-Nada, Eiyad, and Ali J. Chamkha. 2010. "Mixed Convection Flow in a Lid-Driven Inclined Square Enclosure Filled with a Nanofluid." *European Journal of Mechanics, B/Fluids* 29 (6): 472–82.
- Adrian Bejan. 2013. *Convection heat transfer*. Fourth edi.
- Ahmed Sameh E, Raizah Zehba A.S., Aly Abdelraheem M. 2020. "Magnetohydrodynamic Convective Flow Of Nanofluid In Double Liddriven Cavities Under Slip Conditions." *Thermal Science*, 141–141.
- Ahmed, Sameh E., M. A. Mansour, and A. Mahdy. 2013. "MHD Mixed Convection in an Inclined Lid-Driven Cavity with Opposing Thermal Buoyancy Force: Effect of Non-Uniform Heating on Both Side Walls." *Nuclear Engineering and Design* 265: 938–48.
- Ahmed, Sameh E. 2020. "Caputo Fractional Convective Flow in an Inclined Wavy Vented Cavity Filled with a Porous Medium Using Al₂O₃-Cu Hybrid Nanofluids." *International Communications in Heat and Mass Transfer* 116 (June): 104690.
- Ahmed, Sameh E, M A Mansour, Anas M Alwatban, and Abdelraheem M Aly. 2020. "Finite Element Simulation for MHD Ferro-Convective Flow in an Inclined Double-Lid Driven L-Shaped Enclosure with Heated Corners." *Alexandria Engineering Journal* 59 (1): 217–26.
- Al-Rashed, Abdullah A.A.A., Amin Shahsavar, Mohammad Akbari, Davood Toghraie, Mohammadreza Akbari, and Masoud Afrand. 2019. "Finite Volume Simulation of Mixed Convection in an Inclined Lid-Driven Cavity Filled with Nanofluids: Effects of a Hot Elliptical Centric Cylinder, Cavity Angle and Volume Fraction of Nanoparticles." *Physica A: Statistical Mechanics and Its Applications* 527: 121122.
- Alblawi, Adel, N Zainuddin R Roslan, and Mohammad Rahimi-gorji N A Bakar. 2019. "Effect of Heat Generation on Mixed Convection in Porous Cavity with Sinusoidal Heated Moving Lid and Uniformly Heated or Cooled Bottom Walls."

Microsystem Technologies m (2014).

- Ali Ates, Omer Altun, Adem Kilicman. 2017. "On A Comparison of Numerical Solution Methods for General Transport Equation on Cylindrical Coordinates." *Applied Mathematics and Information Sciences* 11(2): 433–39.
- Ali, Hafiz Muhammad, Hassan Ali, Hassan Liaquat, Hafiz Talha Bin Maqsood, and Malik Ahmed Nadir. 2015. "Experimental Investigation of Convective Heat Transfer Augmentation for Car Radiator Using ZnO-water Nanofluids." *Energy* 84: 317–24.
- Ali, Hafiz Muhammad, Adeel Arshad, Mark Jabbal, and P. G. Verdin. 2018. "Thermal Management of Electronics Devices with PCMs Filled Pin-Fin Heat Sinks: A Comparison." *International Journal of Heat and Mass Transfer* 117: 1199–1204.
- Ali, Hafiz Muhammad, Muhammad Mustafa Generous, Faseeh Ahmad, and Muhammad Irfan. 2017. "Experimental Investigation of Nucleate Pool Boiling Heat Transfer Enhancement of TiO₂-water Based Nanofluids." *Applied Thermal Engineering* 113: 1146–51.
- Alinia, M, D D Ganji, and M Gorji-Bandpy. 2011. "Numerical Study of Mixed Convection in an Inclined Two Sided Lid Driven Cavity Filled with Nanofluid Using Two-Phase Mixture Model." *International Communications in Heat and Mass Transfer* 38 (10): 1428–35.
- Alsabery, Ammar I., Taher Armaghani, Ali J. Chamkha, Muhammad Adil Sadiq, and Ishak Hashim. 2019. "Effects of Two-Phase Nanofluid Model on Convection in a Double Lid-Driven Cavity in the Presence of a Magnetic Field." *International Journal of Numerical Methods for Heat and Fluid Flow* 29 (4): 1272–99.
- Alsabery, Ammar I., Ishak Hashim, Ahmad Hajjar, Mohammad Ghalambaz, Sohail Nadeem, and Mohsen Saffari Pour. 2020. "Entropy Generation and Natural Convection Flow of Hybrid Nanofluids in a Partially Divided Wavy Cavity Including Solid Blocks." *Energies* 13 (11): 2942.
- Alsabery, Ammar I., Muneer A. Ismael, Ali J. Chamkha, and Ishak Hashim. 2018. "Mixed Convection of Al₂O₃-water Nanofluid in a Double Lid-Driven Square Cavity with a Solid Inner Insert Using Buongiorno's Two-Phase Model." *International Journal of Heat and Mass Transfer* 119: 939–61.
- Alsabery, Ammar I, Taher Armaghani, Ali J Chamkha, and Ishak Hashim. 2019. "Two-Phase Nanofluid Model and Magnetic Field Effects on Mixed Convection in a Lid-Driven Cavity Containing Heated Triangular Wall." *Alexandria*

Engineering Journal.

- Alsabery, Ammar I, Tahar Tayebi, Hakim T Kadhim, Mohammad Ghalambaz, Ishak Hashim, and Ali J Chamkha. 2020. "Impact of Two-Phase Hybrid Nanofluid Approach on Mixed Convection inside Wavy Lid-Driven Cavity Having Localized Solid Block." *Journal of Advanced Research*, no. xxxx.
- Aminossadati, S. M., A. Kargar, and B. Ghasemi. 2012. "Adaptive Network-Based Fuzzy Inference System Analysis of Mixed Convection in a Two-Sided Lid-Driven Cavity Filled with a Nanofluid." *International Journal of Thermal Sciences* 52 (1): 102–11.
- Arefmanesh, Ali, and Mostafa Mahmoodi. 2011. "Effects of Uncertainties of Viscosity Models for Al_2O_3 -water Nanofluid on Mixed Convection Numerical Simulations." *International Journal of Thermal Sciences* 50 (9): 1706–19. <https://doi.org/10.1016/j.ijthermalsci.2011.04.007>.
- Arshad, Adeel, Hafiz Muhammad Ali, Muzaffar Ali, and Shehryar Manzoor. 2017. "Thermal Performance of Phase Change Material (PCM) Based Pin-Finned Heat Sinks for Electronics Devices: Effect of Pin Thickness and PCM Volume Fraction." *Applied Thermal Engineering* 112: 143–55.
- Arshad, Adeel, Hafiz Muhammad Ali, Shahab Khushnood, and Mark Jabbal. 2018. "Experimental Investigation of PCM Based Round Pin-Fin Heat Sinks for Thermal Management of Electronics: Effect of Pin-Fin Diameter." *International Journal of Heat and Mass Transfer* 117: 861–72.
- Arshad, Waqas, and Hafiz Muhammad Ali. 2017. "Graphene Nanoplatelets Nanofluids Thermal and Hydrodynamic Performance on Integral Fin Heat Sink." *International Journal of Heat and Mass Transfer* 107: 995–1001.
- Ashraf, Muhammad Junaid, Hafiz Muhammad Ali, Hazrat Usman, and Adeel Arshad. 2017. "Experimental Passive Electronics Cooling: Parametric Investigation of Pin-Fin Geometries and Efficient Phase Change Materials." *International Journal of Heat and Mass Transfer* 115: 251–63.
- Asiaei, Sasan, Ali Zadehkafi, and Majid Siavashi. 2018. "Multi-Layered Porous Foam Effects on Heat Transfer and Entropy Generation of Nanofluid Mixed Convection Inside a Two-Sided Lid-Driven Enclosure with Internal Heating." *Transport in Porous Media*.
- Ataka, Mitsuo, and Nobuko I Wakayama. 2002. "Effects of a Magnetic Field and Magnetization Force on Protein Crystal Growth. Why Does a Magnet Improve

the Quality of Some Crystals?" *Acta Crystallographica. Section D, Biological Crystallography* 58 (Pt 10 Pt 1): 1708–10.

- Azizul, Fatin M., Ammar I. Alsabery, and Ishak Hashim. 2020. "Heatlines Visualisation of Mixed Convection Flow in a Wavy Heated Cavity Filled with Nanofluids and Having an Inner Solid Block." *International Journal of Mechanical Sciences* 175 (October 2019): 105529.
- Azizul, Fatin M, Ammar I Alsabery, Ishak Hashim, and Ali J Chamkha. 2020. "Heatline Visualization of Mixed Convection inside Double Lid-Driven Cavity Having Heated Wavy Wall." *Journal of Thermal Analysis and Calorimetry*.
- B. Gebhart, y. Jaluria, r. L. Mahajan and b. Sammakia. 1988. *Buoyancy-Induced Flows and Transport*.
- Baby, Tessy Theres, and Sundara Ramaprabhu. 2011. "Synthesis and Nanofluid Application of Silver Nanoparticles Decorated Graphene." *Journal of Materials Chemistry* 21 (26): 9702–9.
- Baby, Tessy Theres, and Ramaprabhu Sundara. 2011. "Synthesis and Transport Properties of Metal Oxide Decorated Graphene Dispersed Nanofluids." *Journal of Physical Chemistry C* 115 (17): 8527–33.
- Barnoon, Pouya, Davood Toghraie, Reza Balali Dehkordi, and Hossein Abed. 2019. "MHD Mixed Convection and Entropy Generation in a Lid-Driven Cavity with Rotating Cylinders Filled by a Nanofluid Using Two Phase Mixture Model." *Journal of Magnetism and Magnetic Materials* 483 (February): 224–48.
- Basak, Tanmay, and Ali J. Chamkha. 2012. "Heatline Analysis on Natural Convection for Nanofluids Confined within Square Cavities with Various Thermal Boundary Conditions." *International Journal of Heat and Mass Transfer* 55 (21–22): 5526–43.
- Basak, Tanmay, S. Roy, and A. R. Balakrishnan. 2006. "Effects of Thermal Boundary Conditions on Natural Convection Flows within a Square Cavity." *International Journal of Heat and Mass Transfer* 49 (23–24): 4525–35.
- Basak, Tanmay, S. Roy, Sandeep Kumar Singh, and I. Pop. 2010. "Analysis of Mixed Convection in a Lid-Driven Porous Square Cavity with Linearly Heated Side Wall(S)." *International Journal of Heat and Mass Transfer* 53 (9–10): 1819–40.
- Basak, Tanmay, S Roy, and A J Chamkha. 2012. "A Peclet Number Based Analysis of Mixed Convection for Lid-Driven Porous Square Cavities with Various Heating of Bottom Wall ☆." *International Communications in Heat and Mass*

Transfer 39 (5): 657–64.

- Basak, Tanmay, S Roy, Pawan Kumar, and I Pop. 2009. “Analysis of Mixed Convection Flows within a Square Cavity with Uniform and Non-Uniform Heating of Bottom Wall.” *International Journal of Thermal Sciences* 48 (5): 891–912.
- Bhuvaneshwari, M., S. Sivasankaran, and Y. J. Kim. 2011. “Magnetoconvection in a Square Enclosure with Sinusoidal Temperature Distributions on Both Side Walls.” *Numerical Heat Transfer; Part A: Applications* 59 (3): 167–84.
- Bilgen, E., and R. Ben Yedder. 2007. “Natural Convection in Enclosure with Heating and Cooling by Sinusoidal Temperature Profiles on One Side.” *International Journal of Heat and Mass Transfer* 50 (1–2): 139–50.
- Bondarenko, Darya S, Mikhail A Sheremet, Hakan F Oztop, and Nidal Abu-hamdeh. 2018. “Mixed Convection Heat Transfer of a Nanofluid in a Lid-Driven Enclosure with Two Adherent Porous Blocks.” *Journal of Thermal Analysis and Calorimetry* 9.
- Boulaia, Zoubair, Abderrahim Wakif, and Rachid Sehaqui. 2016. “Numerical Study of Mixed Convection of the Nanofluids in Two-Sided Lid-Driven Square Cavity with a Pair of Triangular Heating Cylinders.” *Journal of Engineering* 2016: 8.
- C. Y. SOONG and P. Y. TZENG. 1996. “Numerical Study on Mode-Transition of Natural Convection in Differentially Heated Inclined Enclosures.” *International Journal of Heat Mass Transfer*. 39: 869–2882.
- Calcagni, B, F Marsili, and M Paroncini. 2005. “Natural Convective Heat Transfer in Square Enclosures Heated from Below.” *Applied Thermal Engineering* 25: 2522–31.
- Carmichael, L. T., Virginia Berry, and B. H. Sage. 1963. “Thermal Conductivity of Fluids. Ethane.” *Journal of Chemical and Engineering Data*. 3:281–285.
- Chamkha, A. J., A. M. Rashad, T. Armaghani, and M. A. Mansour. 2018. “Effects of Partial Slip on Entropy Generation and MHD Combined Convection in a Lid-Driven Porous Enclosure Saturated with a Cu–water Nanofluid.” *Journal of Thermal Analysis and Calorimetry* 132 (2): 1291–1306.
- Chamkha, Ali J, and Eiyad Abu-Nada. 2012. “Mixed Convection Flow in Single- and Double-Lid Driven Square Cavities Filled with water– Al₂O₃ Nanofluid: Effect of Viscosity Models.” *European Journal of Mechanics - B/Fluids* 36: 82–96.
- Chamkha, Ali J, Fatih Selimefendigil, and Hakan F Oztop. 2020. “Effects of a Rotating

- Cone on the Mixed Convection in a Double Lid-Driven 3D Porous Trapezoidal Nanofluid Filled Cavity under the Impact of Magnetic Field.” *Nanomaterials*, 1–18.
- Chatterjee, Dipankar, Satish Kumar, and Bittagopal Mondal. 2014. “Mixed Convective Transport in a Lid-Driven Cavity Containing a Nano Fluid and a Rotating Circular Cylinder at the Center ☆.” *International Communications in Heat and Mass Transfer* 56: 71–78.
- Chattopadhyay, Anirban, Swapan K. Pandit, Sreejata Sen Sarma, and I. Pop. 2016. “Mixed Convection in a Double Lid-Driven Sinusoidally Heated Porous Cavity.” *International Journal of Heat and Mass Transfer* 93: 361–78.
- Cho, Ching-chang. 2019. “International Journal of Mechanical Sciences Mixed Convection Heat Transfer and Entropy Generation of Cu-water Nanofluid in Wavy-Wall Lid-Driven Cavity in Presence of Inclined Magnetic Field.” *International Journal of Mechanical Sciences* 151 (December 2018): 703–14.
- Cimpean, D. S., M. A. Sheremet, and I. Pop. 2020. “Mixed Convection of Hybrid Nanofluid in a Porous Trapezoidal Chamber.” *International Communications in Heat and Mass Transfer* 116: 104627.
- Cimpean, D S, and M A Sheremet. 2020. “Mixed Convection of Hybrid Nanofluid in a Porous Trapezoidal Chamber.” *International Communications in Heat and Mass Transfer* 116 (May): 104627.
- Corcione, Massimo. 2011. “Empirical Correlating Equations for Predicting the Effective Thermal Conductivity and Dynamic Viscosity of Nanofluids.” *Energy Conversion and Management* 52 (1): 789–93.
- Corvaro, F., and M. Paroncini. 2007. “Experimental Analysis of Natural Convection in Square Cavities Heated from below with 2D-PIV and Holographic Interferometry Techniques.” *Experimental Thermal and Fluid Science* 31 (7): 721–39.
- Das, Pritam Kumar, Arnab Kumar Mallik, Ranjan Ganguly, and Apurba Kumar Santra. 2016. “Synthesis and Characterization of TiO₂-water Nanofluids with Different Surfactants.” *International Communications in Heat and Mass Transfer* 75: 341–48.
- Deng, Qi Hong, and Juan Juan Chang. 2008. “Natural Convection in a Rectangular Enclosure with Sinusoidal Temperature Distributions on Both Side Walls.” *Numerical Heat Transfer; Part A: Applications* 54 (5): 507–24.

- Donald A. Nield, Adrian Bejan. 1999. *Convection in Porous Media*.
- Ellahi, Saeed Nazari R, M M Sarafraz Mohammad, Reza Safaei, Ali Asgari, and Omid Ali. 2019. "Numerical Study on Mixed Convection of a Non-Newtonian Nanofluid with Porous Media in a Two Lid-Driven Square Cavity." *Journal of Thermal Analysis and Calorimetry* 1 (m).
- Elshehabey, Hillal M, and Sameh E Ahmed. 2015. "International Journal of Heat and Mass Transfer MHD Mixed Convection in a Lid-Driven Cavity Filled by a Nanofluid with Sinusoidal Temperature Distribution on the Both Vertical Walls Using Buongiorno ' s Nanofluid Model." *HEAT AND MASS TRANSFER* 88: 181–202.
- Esfahani, J A, M Akbarzadeh, S Rashidi, M A Rosen, and R Ellahi. 2017. "Influences of Wavy Wall and Nanoparticles on Entropy Generation over Heat Exchanger Plat." *International Journal of Heat and Mass Transfer* 109: 1162–71.
- Esfahani, Masihollah Ahmadi, and Davood Toghraie. 2017. "Experimental Investigation for Developing a New Model for the Thermal Conductivity of Silica/water-Ethylene Glycol (40%–60%) Nanofluid at Different Temperatures and Solid Volume Fractions." *Journal of Molecular Liquids* 232: 105–12.
- Esfandiary, Meissam, Babak Mehmandoust, Arash Karimipour, and Hossein Ali Pakravan. 2016. "Natural Convection of Al_2O_3 –water Nanofluid in an Inclined Enclosure with the Effects of Slip Velocity Mechanisms: Brownian Motion and Thermophoresis Phenomenon." *International Journal of Thermal Sciences* 105: 137–58.
- Fakheri, Ahmad. 2014. *Intermediate Heat Transfer*.
- Farbod, Mansoor, and Ameneh Ahangarpour. 2016. "Improved Thermal Conductivity of Ag Decorated Carbon Nanotubes water Based Nanofluids." *Physics Letters, Section A: General, Atomic and Solid State Physics* 380 (48): 4044–48.
- Gangawane, Krunal M, Hakan F Oztop, and Mohamed E Ali. 2019. "International Journal of Mechanical Sciences Mixed Convection in a Lid-Driven Cavity Containing Triangular Block with Constant Heat Flux : Effect of Location of Block." *International Journal of Mechanical Sciences* 152 (August 2018): 492–511.
- Garmroodi, M R Daneshvar, A Ahmadpour, and F Talati. 2019. "International Journal of Mechanical Sciences MHD Mixed Convection of Nanofluids in the Presence of Multiple Rotating Cylinders in Different Configurations : A Two-Phase

- Numerical Study.” *International Journal of Mechanical Sciences* 150 (March 2018): 247–64.
- Garoosi, Faroogh, and Mohammad Mehdi Rashidi. 2017. “Conjugate-Mixed Convection Heat Transfer in a Two-Sided Lid-Driven Cavity Filled with Nanofluid Using Manninen’s Two Phase Model.” *International Journal of Mechanical Sciences* 131–132 (July): 1026–48.
- Garoosi, Faroogh, Behzad Rohani, and Mohammad Mehdi Rashidi. 2015. “Two-Phase Mixture Modeling of Mixed Convection of Nanofluids in a Square Cavity with Internal and External Heating.” *Powder Technology* 275: 304–21.
- Ghaffarpasand, Omid. 2016. “Numerical Study of MHD Natural Convection inside a Sinusoidally Heated Lid-Driven Cavity Filled with Fe_3O_4 -water Nanofluid in the Presence of Joule Heating.” *Applied Mathematical Modelling* 40 (21): 9165–82.
- Ghasemi, B., and S. M. Aminossadati. 2009. “Natural Convection Heat Transfer in an Inclined Enclosure Filled with a water-Cuo Nanofluid.” *Numerical Heat Transfer; Part A: Applications* 55 (8): 807–23.
- Ghasemi, B, S M Aminossadati, and A Raisi. 2011. “Magnetic Field Effect on Natural Convection in a Nanofluid-Filled Square Enclosure.” *International Journal of Thermal Sciences* 50 (9): 1748–56.
- Ghasemi, Kasra, and Majid Siavashi. 2020. “International Journal of Mechanical Sciences Three-Dimensional Analysis of Magnetohydrodynamic Transverse Mixed Convection of Nanofluid inside a Lid-Driven Enclosure Using MRT-LBM.” *International Journal of Mechanical Sciences* 165 (September 2019): 105199.
- Gibanov, Nikita S., Mikhail A. Sheremet, Hakan F. Oztop, and Nidal Abu-Hamdeh. 2017. “Effect of Uniform Inclined Magnetic Field on Mixed Convection in a Lid-Driven Cavity Having a Horizontal Porous Layer Saturated with a Ferrofluid.” *International Journal of Heat and Mass Transfer* 114: 1086–97.
- Gibanov, Nikita S., Mikhail A. Sheremet, Hakan F. Oztop, and Khaled Al-Salem. 2017. “Convective Heat Transfer in a Lid-Driven Cavity with a Heat-Conducting Solid Backward Step under the Effect of Buoyancy Force.” *International Journal of Heat and Mass Transfer* 112: 158–68.
- Goodarzi, M., M. R. Safaei, K. Vafai, G. Ahmadi, M. Dahari, S. N. Kazi, and N. Jomhari. 2014. “Investigation of Nanofluid Mixed Convection in a Shallow Cavity Using a Two-Phase Mixture Model.” *International Journal of Thermal*

Sciences 75: 204–20.

Hamid, M. 2020. “Finite Element Analysis of Hybrid Nanofluid Flow and Heat Transfer in a Split Lid-Driven Square Cavity with Y-Shaped Obstacle Finite Element Analysis of Hybrid Nanofluid Flow and Heat Transfer in a Split Lid-Driven Square Cavity with Y-Shaped Obstacle” 093609 (July).

Harlow, Francis H.; Welch, J. Eddie. 1965. “Numerical Calculation of Time-Dependent Viscous Incompressible Flow of Fluid with Free Surfaces.” *Physics of Fluids* 8 (12): 2182–89.

Hemmat Esfe, Mohammad, Ali Akbar Abbasian Arani, Mohammad Rezaie, Wei Mon Yan, and Arash Karimipour. 2015. “Experimental Determination of Thermal Conductivity and Dynamic Viscosity of Ag-MgO/water Hybrid Nanofluid.” *International Communications in Heat and Mass Transfer* 66: 189–95.

Hemmat, Mohammad, Mohammad Akbari, Arash Karimipour, and Masoud Afrand. 2015. “International Journal of Heat and Mass Transfer Mixed-Convection Flow and Heat Transfer in an Inclined Cavity Equipped to a Hot Obstacle Using Nanofluids Considering Temperature-Dependent Properties.” *HEAT AND MASS TRANSFER* 85: 656–66.

Henk Kaarle Versteeg, Weeratunge Malalasekera. 2007. *An Introduction to Computational Fluid Dynamics: The Finite Volume Method*.

Huminić, Gabriela, and Angel Huminić. 2017. “Numerical Analysis of Hybrid Nanofluids as Coolants for Automotive Applications.” *International Journal of Heat and Technology* 35 (Special Issue 1): S288–92.

Huminić, Gabriela Huminić, Angel. 2018. “The Heat Transfer Performances and Entropy Generation Analysis of Hybrid Nanofluids in a Flattened Tube.” *International Journal of Heat and Mass Transfer* 119: 813–27.

Hussain, S., S. Ahmad, K. Mehmood, and M. Sagheer. 2017. “Effects of Inclination Angle on Mixed Convective Nanofluid Flow in a Double Lid-Driven Cavity with Discrete Heat Sources.” *International Journal of Heat and Mass Transfer* 106: 847–60.

Hussain, S, S Ahmad, K Mehmood, and M Sagheer. 2017. “Effects of Inclination Angle on Mixed Convective Nanofluid Flow in a Double Lid-Driven Cavity with Discrete Heat Sources.” *International Journal of Heat and Mass Transfer* 106: 847–60.

Hussain, S, K Mehmood, and M Sagheer. 2016. “MHD Mixed Convection and

- Entropy Generation of water–Alumina Nanofluid Flow in a Double Lid Driven Cavity with Discrete Heating.” *Journal of Magnetism and Magnetic Materials* 419: 140–55.
- Hussain, Salam Hadi, Ahmed Kadhim Hussein, and Rehab Noor Mohammed. 2012. “Studying the Effects of a Longitudinal Magnetic Field and Discrete Isoflux Heat Source Size on Natural Convection inside a Tilted Sinusoidal Corrugated Enclosure.” *Computers and Mathematics with Applications* 64 (4): 476–88.
- Hussain, Shafqat, Muhammad Jamal, and B Pekmen Geridonmez. 2020. “Impact of Fins and Inclined Magnetic Field in Double Lid-Driven Cavity with Cu–water Nanofluid.” *International Journal of Thermal Sciences*, 106707.
- I., Alsabery Ammar, Armaghani Taher, Chamkha Ali J., Sadiq Muhammad Adil, and Hashim Ishak. 2019. “Effects of Two-Phase Nanofluid Model on Convection in a Double Lid-Driven Cavity in the Presence of a Magnetic Field.” *International Journal of Numerical Methods for Heat and Fluid Flow* 29 (4): 1272–99.
- Ismael, Muneer A., T. Armaghani, A J Chamkha. 2018. “Mixed Convection And Entropy Generation In A Lid-Driven Cavity Filled With A Hybrid Nanofluid And Heated By A Triangular Solid.” *Heat Transfer Research* 49 (17). 1645-1665.
- Ismael, Muneer A., Ioan Pop, and Ali J. Chamkha. 2014. “Mixed Convection in a Lid-Driven Square Cavity with Partial Slip.” *International Journal of Thermal Sciences* 82 (1): 47–61.
- Izadi, Mohsen, Amin Behzadmehr, and Mohammad Mohsen Shahmardan. 2014. “Effects of Discrete Source-Sink Arrangements on Mixed Convection in a Square Cavity Filled by Nanofluid.” *Korean Journal of Chemical Engineering* 31 (1): 12–19.
- Izadi, Sina, Taher Armaghani, Ramin Ghasemiasl, Ali J Chamkha, and Maysam Molana. 2019. “A Comprehensive Review on Mixed Convection of Nanofluids in Various Shapes of Enclosures.” *Powder Technology* 343: 880–907.
- Jajja, Saad Ayub, Wajahat Ali, and Hafiz Muhammad Ali. 2014. “Multiwalled Carbon Nanotube Nanofluid for Thermal Management of High Heat Generating Computer Processor.” *Heat Transfer - Asian Research* 43 (7): 653–66.
- Jakeer, Shaik, P Balaanki Reddy, A M Rashad, and Hossam A Nabwey. 2020. “Impact of Heated Obstacle Position on Magneto-Hybrid Nanofluid Flow in a Lid-Driven Porous Cavity with Cattaneo-Christov Heat Flux Pattern.” *Alexandria Engineering Journal*.

- Jamesahar, Esmail, Mahmoud Sabour, Mohammad Shahabadi, S. A.M. Mehryan, and Mohammad Ghalambaz. 2020. "Mixed Convection Heat Transfer by Nanofluids in a Cavity with Two Oscillating Flexible Fins: A Fluid–Structure Interaction Approach." *Applied Mathematical Modelling* 82: 72–90.
- Jena, P. K., E. A. Brocchi, and M. S. Motta. 2001. "In-Situ Formation of Cu-Al₂O₃ Nano-Scale Composites by Chemical Routes and Studies on Their Microstructures." *Materials Science and Engineering A* 313 (1–2): 180–86.
- Jmai, Ridha, Brahim Ben-Beya, and Taieb Lili. 2016. "Numerical Analysis of Mixed Convection at Various Walls Speed Ratios in Two-Sided Lid-Driven Cavity Partially Heated and Filled with Nanofluid." *Journal of Molecular Liquids* 221: 691–713.
- Karim, Azharul, M. Masum Billah, M. T. Talukder Newton, and M. Mustafizur Rahman. 2017. "Influence of the Periodicity of Sinusoidal Boundary Condition on the Unsteady Mixed Convection within a Square Enclosure Using an Ag-water Nanofluid." *Energies* 10 (12).
- Karimipour, A., A. H. Nezhad, A. Behzadmehr, S. Alikhani, and E. Abedini. 2011. "Periodic Mixed Convection of a Nanofluid in a Cavity with Top Lid Sinusoidal Motion." *Proceedings of the Institution of Mechanical Engineers, Part C: Journal of Mechanical Engineering Science* 225 (9): 2149–60.
- Karimipour, Arash, Mohammad Hemmat Esfe, Mohammad Reza Safaei, Davood Toghraie Semiromi, Saeed Jafari, and S. N. Kazi. 2014. "Mixed Convection of Copper-water Nanofluid in a Shallow Inclined Lid Driven Cavity Using the Lattice Boltzmann Method." *Physica A: Statistical Mechanics and Its Applications* 402 (xxxx): 150–68.
- Kashyap, Dhrubajyoti, and Anoop K Dass. 2019. "International Journal of Mechanical Sciences Effect of Boundary Conditions on Heat Transfer and Entropy Generation during Two-Phase Mixed Convection Hybrid Al₂O₃-Cu / water Nanofluid Flow in a Cavity" 158 (December 2018): 45–59.
- Kefayati, G H R. 2017. "Mixed Convection of Non-Newtonian Nanofluid in an Enclosure Using Buongiorno's Mathematical Model." *International Journal of Heat and Mass Transfer* 108: 1481–1500.
- Kefayati, GH H.R., and H. Tang. 2018. "MHD Mixed Convection of Viscoplastic Fluids in Different Aspect Ratios of a Lid-Driven Cavity Using LBM." *International Journal of Heat and Mass Transfer* 124: 344–67.

- Kefayati, Gh R. 2015. "FDLBM Simulation of Mixed Convection in a Lid-Driven Cavity Filled with Non-Newtonian Nanofluid in the Presence of Magnetic Field." *International Journal of Thermal Sciences* 95: 29–46.
- Khanafer, Khalil M., Abdalla M. Al-Amiri, and Ioan Pop. 2007. "Numerical Simulation of Unsteady Mixed Convection in a Driven Cavity Using an Externally Excited Sliding Lid." *European Journal of Mechanics, B/Fluids*.
- Khanafer, Khalil, Kambiz Vafai, and Marilyn Lightstone. 2003. "Buoyancy-Driven Heat Transfer Enhancement in a Two-Dimensional Enclosure Utilizing Nanofluids." *International Journal of Heat and Mass Transfer* 46 (19): 3639–53.
- Khorasanizadeh, H., M. Nikfar, and J. Amani. 2013. "Entropy Generation of Cu-water Nanofluid Mixed Convection in a Cavity." *European Journal of Mechanics, B/Fluids* 37: 143–52.
- Lamarti, H, M Mahdaoui, R Bennacer, and A Chahboun. 2019. "International Journal of Heat and Mass Transfer Numerical Simulation of Mixed Convection Heat Transfer of Fluid in a Cavity Driven by an Oscillating Lid Using Lattice Boltzmann Method." *International Journal of Heat and Mass Transfer* 137: 615–29.
- Li, Zhixiong, Pouya Barnoon, Davood Toghraie, Reza Balali Dehkordi, and Masoud Afrand. 2019. "Mixed Convection of Non-Newtonian Nanofluid in an H-Shaped Cavity with Cooler and Heater Cylinders Filled by a Porous Material: Two Phase Approach." *Advanced Powder Technology* 30 (11): 2666–85.
- Louaraychi, A., M. Lamsaadi, M. Naïmi, H. El Harfi, M. Kaddiri, A. Raji, and M. Hasnaoui. 2019. "Mixed Convection Heat Transfer Correlations in Shallow Rectangular Cavities with Single and Double-Lid Driven Boundaries." *International Journal of Heat and Mass Transfer* 132: 394–406.
- Mahmoodi, Mostafa. 2011. "Mixed Convection inside Nanofluid Filled Rectangular Enclosures with Moving Bottom Wall." *Thermal Science* 15 (3): 889–903.
- Mahmoudi, Amir Houshang, Ioan Pop, and Mina Shahi. 2012. "Effect of Magnetic Field on Natural Convection in a Triangular Enclosure Filled with Nanofluid." *International Journal of Thermal Sciences* 59: 126–40.
- Manchanda, Manvi, and Krunal M. Gangawane. 2018. "Mixed Convection in a Two-Sided Lid-Driven Cavity Containing Heated Triangular Block for Non-Newtonian Power-Law Fluids." *International Journal of Mechanical Sciences* 144 (January): 235–48.

- Mansour, M. A., R. A. Mohamed, M. M. Abd-Elaziz, and Sameh E. Ahmed. 2010. "Numerical Simulation of Mixed Convection Flows in a Square Lid-Driven Cavity Partially Heated from below Using Nanofluid." *International Communications in Heat and Mass Transfer* 37 (10): 1504–12.
- Mansour, M A, Sameh E Ahmed, Abdelraheem M Aly, Zehba A S Raizah, and Z Morsy. 2020. "Triple Convective Flow of Micropolar Nanofluids in Double Lid-Driven Enclosures Partially Filled with LTNE Porous Layer under Effects of an Inclined Magnetic Field." *Chinese Journal of Physics* 68 (May): 387–405.
- Martynenko, Oleg G., Khramtsov, Pavel P. 2005. *Free-Convective Heat Transfer*.
- Massey, Bernard. 2006. *Mechanics of Fluids*.
- Mazrouei, Saeed, Mostafa Mahmoodi, and Seyed Mohammad. 2012. "International Journal of Thermal Sciences Effect of Nano Fluid Variable Properties on Mixed Convection in a Square Cavity." *International Journal of Thermal Sciences* 52: 112–26.
- Megatif, Lena, A. Ghozatloo, A. Arimi, and M. Shariati-Niasar. 2016. "Investigation of Laminar Convective Heat Transfer of a Novel TiO₂-Carbon Nanotube Hybrid water-Based Nanofluid." *Experimental Heat Transfer* 29 (1): 124–38.
- Mehmood, K. Hussain, S. Sagheer, M. 2017. "Numerical Simulation of MHD Mixed Convection in Alumina–water Nanofluid Filled Square Porous Cavity Using KKL Model: Effects of Non-Linear Thermal Radiation and Inclined Magnetic Field." *Journal of Molecular Liquids* 238: 485–98.
- Mehmood, K., S. Hussain, and M. Sagheer. 2017. "Mixed Convection in Alumina-water Nanofluid Filled Lid-Driven Square Cavity with an Isothermally Heated Square Blockage inside with Magnetic Field Effect: Introduction." *International Journal of Heat and Mass Transfer* 109: 397–409.
- Minea, Alina Adriana. 2017a. "Challenges in Hybrid Nanofluids Behavior in Turbulent Flow: Recent Research and Numerical Comparison." *Renewable and Sustainable Energy Reviews* 71 (December): 426–34.
- Minea, Alina Adriana. 2017b. "Hybrid Nanofluids Based on Al₂O₃, TiO₂ and SiO₂: Numerical Evaluation of Different Approaches." *International Journal of Heat and Mass Transfer* 104: 852–60.
- Mintsa, Honorine Angue, Gilles Roy, Cong Tam Nguyen, and Dominique Doucet. 2009. "New Temperature Dependent Thermal Conductivity Data for water-Based Nanofluids." *International Journal of Thermal Sciences* 48 (2): 363–71.

- Morzynski, M., and Cz O. Popiel. 1988. "Laminar Heat Transfer in a Two-Dimensional Cavity Covered by a Moving Wall." *Numerical Heat Transfer* 13 (2): 265–73.
- Muhammad, Noor, S Nadeem, and Alibek Issakhov. 2020. "Finite Volume Method for Mixed Convection Flow of Ag – Ethylene Glycol Nanofluid Flow in a Cavity Having Thin Central Heater." *Physica A* 537: 122738.
- Muthamilselvan, M, and Deog Hee. 2014. "Mixed Convection of Heat Generating Nanofluid in a Lid-Driven Cavity with Uniform and Non-Uniform Heating of Bottom Wall." *Applied Mathematical Modelling* 38 (13): 3164–74.
- N. B. Vargaftik. 1993. *Handbook of Thermal Conductivity of Liquids and Gases*.
- Nazeer, Mubbashar, Nasir Ali, Tariq Javed, and Mudassar Razzaq. 2019. "Finite Element Simulations for Energy Transfer in a Lid-Driven Porous Square Container Filled with Micropolar Fluid: Impact of Thermal Boundary Conditions and Peclet Number." *International Journal of Hydrogen Energy* 44 (14): 7656–66.
- Nimmagadda, Rajesh, and K. Venkatasubbaiah. 2015. "Conjugate Heat Transfer Analysis of Micro-Channel Using Novel Hybrid Nanofluids ($\text{Al}_2\text{O}_3 + \text{Ag} / \text{water}$)." *European Journal of Mechanics, B/Fluids* 52: 19–27.
- Nine, Md J., B. Munkhbayar, M. Sq Rahman, Hanshik Chung, and Hyomin Jeong. 2013. "Highly Productive Synthesis Process of Well Dispersed Cu_2O and $\text{Cu}/\text{Cu}_2\text{O}$ Nanoparticles and Its Thermal Characterization." *Materials Chemistry and Physics* 141 (2–3): 636–42.
- Nosonov, Ivan I., and Mikhail A. Sheremet. 2018. "Conjugate Mixed Convection in a Rectangular Cavity with a Local Heater." *International Journal of Mechanical Sciences* 136 (January): 243–51.
- Nuim Labib, M., Md J. Nine, Handry Afrianto, Hanshik Chung, and Hyomin Jeong. 2013. "Numerical Investigation on Effect of Base Fluids and Hybrid Nanofluid in Forced Convective Heat Transfer." *International Journal of Thermal Sciences* 71: 163–71.
- Oliver, Yeo Pu Zhong. 2011. "Comparison of Finite Difference and Finite Volume Methods Development of an Educational Tool for the Fixed - Bed Gas Adsorption Problem." National University of Singapore.
- Oosthuizen, Patrick H., Kalendar, Abdulrahim Y. 2018. *Natural Convective Heat Transfer from Horizontal and Near Horizontal Surfaces*.

- Ouertatani, Nasreddine, Nader Ben Cheikh, Brahim Ben Beya, Taieb Lili, and Antonio Campo. 2009. "Mixed Convection in a Double Lid-Driven Cubic Cavity." *International Journal of Thermal Sciences* 48 (7): 1265–72.
- Oztop, Hakan F., Eiyad Abu-Nada, Yasin Varol, and Khaled Al-Salem. 2011. "Computational Analysis of Non-Isothermal Temperature Distribution on Natural Convection in Nanofluid Filled Enclosures." *Superlattices and Microstructures* 49 (4): 453–67.
- P. A. Davidson. 2001. *An Introduction to Magnetohydrodynamics*. Cambridge University Press.
- P. Selvakumar, S. Suresh. 2012. "Use of Al₂O₃-Cu/water Hybrid Nanofluid in an Electronic Heat Sink." *IEEE Transactions on Components, Packaging and Manufacturing Technology* 2 (10): 1600–1607.
- Pal, S. K., S. Bhattacharyya, and I. Pop. 2018. "Effect of Solid-to-Fluid Conductivity Ratio on Mixed Convection and Entropy Generation of a Nanofluid in a Lid-Driven Enclosure with a Thick Wavy Wall." *International Journal of Heat and Mass Transfer* 127: 885–900.
- Pijush Kundu Ira Cohen. 2010. *Fluid Mechanics* 4th Edition.
- Pirmohammadi, Mohsen, and Majid Ghassemi. 2009. "Effect of Magnetic Field on Convection Heat Transfer inside a Tilted Square Enclosure." *International Communications in Heat and Mass Transfer* 36 (7): 776–80.
- R. Turcu, Al Darabont, A. Nan, N. Aldea, D. Macovei, D. Bica, L. Vekas, O. Pana, M. L. Soran, A. A. Koos, L. P. Biro. 2006. "New Polypyrrole-Multiwall Carbon Nanotubes Hybrid Materials." *Journal of Optoelectronics and Advanced Materials* 8 (2): 643–47.
- Rabbi, Khan, Moinuddin Shuvo, Rabiul Hasan, and Satyajit Mojumder. 2016. "Numerical Analysis of Mixed Convection in Lid-Driven Cavity Using Non-Newtonian Ferrofluid with Rotating Cylinder Inside." *American Institute of Physics* 040016.
- Rahman, M. M., M. M. Billah, M. Hasanuzzaman, R. Saidur, and N. A. Rahim. 2012. "Heat Transfer Enhancement of Nanofluids in a Lid-Driven Square Enclosure." *Numerical Heat Transfer; Part A: Applications* 62 (12): 973–91.
- Rashad, A. M., Ali J. Chamkha, Muneer A. Ismael, and Taha Salah. 2018. "Magnetohydrodynamics Natural Convection in a Triangular Cavity Filled with a Cu-Al₂O₃/water Hybrid Nanofluid with Localized Heating from below and

- Internal Heat Generation.” *Journal of Heat Transfer* 140 (7).
- Rashad, A. M., M. A. Mansour, T. Armaghani, and A. J. Chamkha. 2019. “MHD Mixed Convection and Entropy Generation of Nanofluid in a Lid-Driven U-Shaped Cavity with Internal Heat and Partial Slip.” *Physics of Fluids* 31 (4).
- Ray, Sudipta, and Dipankar Chatterjee. 2014. “Numerical Heat Transfer , Part A : Applications : An International Journal of Computation and Methodology MHD Mixed Convection in a Lid-Driven Cavity Including Heat Conducting Solid Object and Corner Heaters with Joule Heating,” no. January 2015: 37–41.
- S.V. Patankar. 1980. *Numerical Heat Transfer and Fluid Flow*. Hemisphere, Washington DC.
- Sánchez, D., C. Treviño, and L. Martínez-Suástegui. 2020. “Numerical Study of Magnetohydrodynamic Mixed Convection and Entropy Generation of Al₂O₃-water Nanofluid in a Channel with Two Facing Cavities with Discrete Heating.” *International Journal of Heat and Fluid Flow* 86 (May).
- Sadiq, Muhammad Adil, Ammar I Alsabery, and Ishak Hashim. 2018. “MHD Mixed Convection in a Lid-Driven Cavity with a Bottom Trapezoidal Body : Two-Phase Nanofluid Model.”
- Safaei, Mohammad Reza, Behnam Rahmani, and Marjan Goodarzi. 2011. “Numerical Study of Laminar Mixed Convection Heat Transfer of Power-Law Non-Newtonian Fluids in Square Enclosures by Finite Volume Method.” *International Journal of the Physical Sciences* 6 (33): 7456–70.
- Saha, Goutam. 2010. “Finite Element Simulation of Magnetoconvection inside a Sinusoidal Corrugated Enclosure with Discrete Isoflux Heating from Below.” *International Communications in Heat and Mass Transfer* 37 (4): 393–400.
- Sajid, Muhammad Usman, and Hafiz Muhammad Ali. 2018. “Thermal Conductivity of Hybrid Nanofluids: A Critical Review.” *International Journal of Heat and Mass Transfer* 126: 211–34.
- Sarris, I E, I Lekakis, and N S Vlachos. 2010. “Natural Convection in a 2D Enclosure with Sinusoidal Upper Wall Temperature.” *Numerical Heat Transfer, Part A: Applications* 42 (5): 513–30.
- Sathiyamoorthy, M., Tanmay Basak, S. Roy, and I. Pop. 2007. “Steady Natural Convection Flows in a Square Cavity with Linearly Heated Side Wall(S).” *International Journal of Heat and Mass Transfer* 50 (3–4): 766–75.
- Sathiyamoorthy, M., and Ali Chamkha. 2010. “Effect of Magnetic Field on Natural

- Convection Flow in a Liquid Gallium Filled Square Cavity for Linearly Heated Side Wall(S).” *International Journal of Thermal Sciences* 49 (9): 1856–65.
- Sathiyamoorthy, M., and Ali J. Chamkha. 2012. “Natural Convection Flow under Magnetic Field in a Square Cavity for Uniformly (or) Linearly Heated Adjacent Walls.” *International Journal of Numerical Methods for Heat and Fluid Flow* 22 (5): 677–98.
- Selimefendigil, Fatih, and Hakan F. Öztop. 2016. “Analysis of MHD Mixed Convection in a Flexible Walled and Nanofluids Filled Lid-Driven Cavity with Volumetric Heat Generation.” *International Journal of Mechanical Sciences* 118 (August 2015): 113–24.
- Selimefendigil, Fatih, Hakan F. Oztop, and Ali J. Chamkha. 2019. “MHD Mixed Convection in a Nanofluid Filled Vertical Lid-Driven Cavity Having a Flexible Fin Attached to Its Upper Wall.” *Journal of Thermal Analysis and Calorimetry* 135 (1): 325–40.
- Selimefendigil, Fatih, Hakan F Öztop, and Ali J Chamkha. 2016. “Journal of Magnetism and Magnetic Materials MHD Mixed Convection and Entropy Generation of Nano Fl Uid Fi Lled Lid Driven Cavity under the in Fl Uence of Inclined Magnetic Fi Elds Imposed to Its Upper and Lower Diagonal Triangular Domains,” 1–16.
- Shahi, Mina, Amir Houshang Mahmoudi, and Farhad Talebi. 2011. “A Numerical Investigation of Conjugated-Natural Convection Heat Transfer Enhancement of a Nanofluid in an Annular Tube Driven by Inner Heat Generating Solid Cylinder.” *International Communications in Heat and Mass Transfer* 38 (4): 533–42.
- Sharif, M. A.R. 2007. “Laminar Mixed Convection in Shallow Inclined Driven Cavities with Hot Moving Lid on Top and Cooled from Bottom.” *Applied Thermal Engineering* 27 (5–6): 1036–42.
- Sheikholeslami, M, M Gorji-Bandpy, D D Ganji, and Soheil Soleimani. 2014. “Natural Convection Heat Transfer in a Cavity with Sinusoidal Wall Filled with CuO–water Nanofluid in Presence of Magnetic Field.” *Journal of the Taiwan Institute of Chemical Engineers* 45 (1): 40–49.
- Sheikholeslami, Mohsen. 2018. “CuO-water Nanofluid Flow Due to Magnetic Field inside a Porous Media Considering Brownian Motion.” *Journal of Molecular Liquids* 249: 921–29.

- Sheikhzadeh, G A, M Ebrahim Qomi, N Hajjaligol, and A Fattahi. 2012. "Results in Physics Numerical Study of Mixed Convection Flows in a Lid-Driven Enclosure Filled with Nanofluid Using Variable Properties." RESULTS IN PHYSICS 2: 5–13.
- Sheremet, M A, and I Pop. 2015. "Mixed Convection in a Lid-Driven Square Cavity Filled by a Nanofluid: Buongiorno ' s Mathematical Model." Applied Mathematics and Computation 266: 792–808.
- Shulepova, Elena V, Mikhail A Sheremet, Hakan F Oztop, and Nidal Abu-hamdeh. 2020. "International Journal of Mechanical Sciences Mixed Convection of Al₂O₃ – H₂O Nanoliquid in a Square Chamber with Complicated Fin." International Journal of Mechanical Sciences 165 (September 2019): 105192.
- Sivakumar, V., and S. Sivasankaran. 2014. "Mixed Convection in an Inclined Lid-Driven Cavity with Non-Uniform Heating on Both Sidewalls." Journal of Applied Mechanics and Technical Physics 55 (4): 634–49.
- Sivasankaran, S., A. Malleswaran, Jinho Lee, and Pon Sundar. 2011. "Hydro-Magnetic Combined Convection in a Lid-Driven Cavity with Sinusoidal Boundary Conditions on Both Sidewalls." International Journal of Heat and Mass Transfer 54 (1–3): 512–25.
- Sivasankaran, S., and K. L. Pan. 2012. "Numerical Simulation on Mixed Convection in a Porous Lid-Driven Cavity with Nonuniform Heating on Both Side Walls." Numerical Heat Transfer; Part A: Applications 61 (2): 101–21.
- Sivasankaran, S, V Sivakumar, and P Prakash. 2010. "International Journal of Heat and Mass Transfer Numerical Study on Mixed Convection in a Lid-Driven Cavity with Non-Uniform Heating on Both Sidewalls." International Journal of Heat and Mass Transfer 53 (19–20): 4304–15.
- Streeter, V. L., and E. B. Wylie. 1979. "Fluid Mechanics (Seventh Ed.)."
- Suresh, S., K. P. Venkataraj, P. Selvakumar, and M. Chandrasekar. 2012. "Effect of Al₂O₃-Cu/water Hybrid Nanofluid in Heat Transfer." Experimental Thermal and Fluid Science. Volume 38, April 2012, Pages 54-60
- Suresh, S, K P Venkataraj, M Shahul Hameed, and J Sarangan. 2014. "Turbulent Heat Transfer and Pressure Drop Characteristics of Dilute water Based Al₂O₃ – Cu Hybrid Nanofluids." American Scientific Publishers 14 (3): 2563–72.
- Taghikhani, Mohammad Ali. 2019. "Cu–water Nanofluid MHD Mixed Convection in a Lid-Driven Cavity with Two Sinusoidal Heat Sources Considering Joule

- Heating Effect.” *International Journal of Thermophysics* 40 (4).
- Takabi, Behrouz, and Saeed Salehi. 2014. “Augmentation of the Heat Transfer Performance of a Sinusoidal Corrugated Enclosure by Employing Hybrid Nanofluid.” *Advances in Mechanical Engineering* 2014.
- Takabi, Behrouz, and Hossein Shokouhmand. 2015. “Effects of Al₂O₃-Cu/water Hybrid Nanofluid on Heat Transfer and Flow Characteristics in Turbulent Regime.” *International Journal of Modern Physics C* 26 (4): 1–25.
- Talebi, Farhad, Amir Houshang Mahmoudi, and Mina Shahi. 2010. “Numerical Study of Mixed Convection Flows in a Square Lid-Driven Cavity Utilizing Nanofluid.” *International Communications in Heat and Mass Transfer* 37 (1): 79–90.
- Tayebi, Tahar, Hakan F Öztop, and Ali J Chamkha. 2020. “Natural Convection and Entropy Production in Hybrid Nanofluid Filled-Annular Elliptical Cavity with Internal Heat Generation or Absorption.” *Thermal Science and Engineering Progress* 19: 100605.
- Thakur, Md Shajedul Hoque, Mahmudul Islam, Abrar Ul Karim, Sumon Saha, and Mohammad Nasim Hasan. 2019. “Numerical Study of Laminar Mixed Convection in a Cu-water Nanofluid Filled Lid-Driven Square Cavity with an Isothermally Heated Cylinder.” *AIP Conference Proceedings* 2121 (July).
- Thomas, L.H. 1949. “Elliptic Problems in Linear Differential Equations over a Network.” *Watson Sc. Comp. Lab. Rep.*, Columbia University, New York.
- Tiwari, Raj Kamal, and Manab Kumar Das. 2007. “Heat Transfer Augmentation in a Two-Sided Lid-Driven Differentially Heated Square Cavity Utilizing Nanofluids.” *International Journal of Heat and Mass Transfer* 50 (9–10): 2002–18.
- Toudja, Nihal, Nabila Labsi, Youb Khaled Benkahla, Seif-Eddine Ouyahia, and Mahdi Benzema. 2020. “Thermosolutal Mixed Convection in a Lid-Driven Irregular Hexagon Cavity Filled with MWCNT–MgO (15–85%)/CMC Non-Newtonian Hybrid Nanofluid.” *Journal of Thermal Analysis and Calorimetry*.
- Vahabzadeh Bozorg, Mehdi, and Majid Siavashi. 2019. “Two-Phase Mixed Convection Heat Transfer and Entropy Generation Analysis of a Non-Newtonian Nanofluid inside a Cavity with Internal Rotating Heater and Cooler.” *International Journal of Mechanical Sciences* 151 (December 2018): 842–57.
- Versteeg, H., and Malalasekera, M. 2007. *An Introduction to Computational Fluid Dynamics*. 2nd ed. Pearson.

Wei, Baojie, Changjun Zou, Xihang Yuan, and Xiaoke Li. 2017. "Thermo-Physical Property Evaluation of Diathermic Oil Based Hybrid Nanofluids for Heat Transfer Applications." *International Journal of Heat and Mass Transfer* 107: 281–87.

William S. Janna. 2009. "Engineering Heat Transfer." In , 692.

Zadkhast, Masoud, Davood Toghraie, and Arash Karimipour. 2017. "Developing a New Correlation to Estimate the Thermal Conductivity of MWCNT-CuO/water Hybrid Nanofluid via an Experimental Investigation." *Journal of Thermal Analysis and Calorimetry* 129 (2): 859–67.

